

**Make Better RMS  
Measurements with Your DMM**

Application Note 1392



**Agilent Technologies**

**Who should read  
this application note?**

The application note is for all engineers who need to measure ac voltage.

## Introduction

If you use a digital multimeter (DMM) for ac voltage measurements, it is important to know if your meter is giving you peak value, average value, root-mean-square (rms) value, or something else. If the answer is “something else,” you may be in trouble, and the trouble usually happens with rms measurements.

This application note will help you understand the different techniques DMMs use to measure rms values, how the signal affects the quality of your measurements, and how to avoid common measurement mistakes.

## Measuring rms

Measuring rms values is more complicated than it appears at first glance. If it is complicated, why do we bother? Because true rms is the only ac voltage reading that does not depend on the shape of the signal. It often is the most useful measurement for real-world waveforms.

Often, rms is described as a measure of equivalent heating value, with a relationship to the amount of power dissipated by a resistive load driven by the equivalent dc value. For example, a  $1V_{pk}$  sine wave will deliver the same power to a resistive load as a  $0.707V_{dc}$  signal. A reliable rms reading on a signal will give you a better idea of the effect the signal will have in your circuit.

Figure 1 shows four common voltage parameters. Peak voltage ( $V_{pk}$ ) and peak-to-peak voltage ( $V_{pk-pk}$ ) are simple.  $V_{avg}$  is the average of all the instantaneous values in one complete cycle of the waveform. You will learn how we calculate  $V_{rms}$  below.

For sine waves, the negative half of the waveform cancels out the positive half and averages to zero over one cycle. This type of average would not provide much insight into the signal's effective amplitude, so most meters compute  $V_{avg}$  based on the absolute value of the waveform. For a sine wave, this works out to  $V_{pk} \times 0.637$  (Figure 2).

Figure 1. Common voltage parameters

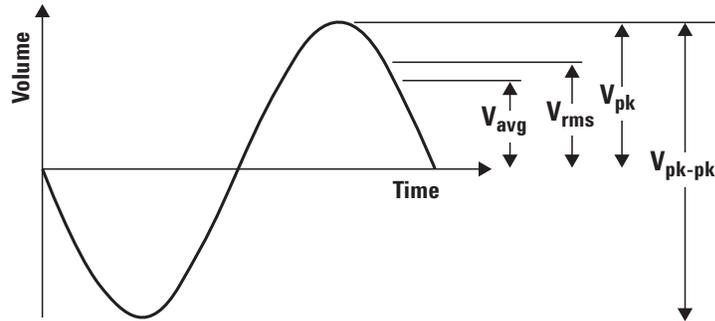
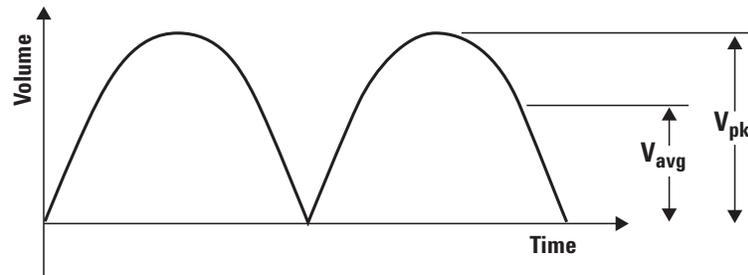


Figure 2.  $V_{avg}$  is calculated based on the absolute value of the waveform.



## Tips for making better rms measurements

You can derive  $V_{\text{rms}}$  by squaring every point in the waveform, finding the average (mean) value of the squares, then finding the square root of the average. With pure sine waves, you can take a couple of shortcuts: just multiply  $V_{\text{pk}} \times 0.707$  or  $V_{\text{avg}} \times 1.11$ . Inexpensive peak-responding or average-responding meters rely on these scaling factors.

The scaling factors apply only to pure sine waves. For every other type of signal, using this approach produces misleading answers. If you are using a meter that is not really designed for the task, you easily can end up with significant error—as high as 40 percent or more—depending on the meter and the signal.

The ratio of  $V_{\text{pk}}$  to  $V_{\text{rms}}$  known as the crest factor, is important to measurement accuracy. The crest factor is a measure of how high the waveform peaks, relative to its RMS value. The higher the crest factor, the more difficult it is to make an accurate ac measurement.

Two measurement challenges are associated with high crest factors. The first involves input range. Imagine a pulse train with a very low duty cycle but a relatively high peak amplitude. Signals like this force the meter to simultaneously measure a high peak value and a much lower rms value, possibly creating overload problems on the high end and resolution problems on the low end.

The second challenge is the amount of higher-frequency energy in the signal. In general, high crest factors indicate more harmonics, which can cause trouble for all meters. Peak- and average-responding meters that are trying to measure rms have a particularly hard time.

Given the importance—and difficulty—of measuring rms, what is the best way to proceed with your day-to-day measurement tasks? The following tips will help you achieve better results.

### **Tip 1:** **Understand how your DMM measures rms.**

When it comes to measuring rms values, multimeters are not created equal. A general understanding of the technology your multimeter uses to measure rms will help you decide if it meets your needs. Here is a summary of the operational advantages and disadvantages of four common multimeter technologies. The first three operate by converting ac to dc; the last one digitizes the analog input signal and then computes rms.

**Thermal ac-to-dc converters** — This older technology for rms measurements uses the equivalent-heating-value approach. The ac signal heats a thermocouple, then the dc section of the meter reads the thermocouple output. Advantages include wide bandwidth and the ability to handle very high crest factors, meaning this approach can deliver true rms for a wide variety of real-world signals.

The disadvantages of the thermal approach are cost and lack of flexibility in trading off measurement speed with low-frequency accuracy. For these reasons, the technique is not used in the latest-generation DMMs.

If you need to measure high-bandwidth and high-crest-factor signals with great accuracy, you may want to search for one of these thermal models. If you are interested in a more contemporary instrument, you may find that the analog ac-to-dc converter technology offers acceptable bandwidth and crest-factor performance, along with superior responsiveness. If high accuracy is important to you, you may want to investigate multimeters that use the digital sampling method.

**Peak and Averaging ac-to-dc converters** — Inexpensive meters, particularly inexpensive hand-held meters, usually derive rms levels from either peak or average values. They deliver true rms only for pure, undistorted sine waves. If you need true rms measurements on real-world signals, these meters are not a viable option.

**Analog ac-to-dc converters** — Many mid-range and high-end DMMs use a chain of analog circuits to compute the square, then the mean, then the square root of the mean to deliver true rms for nearly all signal types. Thanks to advances in integrated circuitry, these DMMs are small, accurate, and still relatively inexpensive.

**Digital sampling** – This last method uses sampling techniques similar to those in digital oscilloscopes to create a set of data points that are sent through an rms algorithm.

Synchronous sampling uses multiple passes to capture a signal as shown in Figure 3. Each subsequent pass is delayed by a small amount, and with enough passes, the signal can be digitized with very high resolution.

This technique has several advantages: true rms on a wide range of signals, high accuracy, and the capability to

create very fast, effective sampling rates and wider bandwidths, even with fairly slow analog-to-digital converters. This method, however, only works with repetitive signals.

If accurate rms measurements are important to you and you are likely to run into pulse trains and other complicated signals, a true rms meter is the only solution. On the other hand, you can save some money with a peak- or average-responding meter. Just keep in mind what these meters can and cannot do.

**Tip 2:**  
**Understand how the signal affects the quality of your measurement.**

Let's look at several different signals, starting with a sine wave. The crest factor for a pure sine wave is 1.414, and a peak-responding meter can provide accurate rms simply by scaling the value of  $V_{pk}$ . With a  $V_{pk}$  value of 500 mV, we expect an rms value around 350 to 357 mV (the range accounts for the inaccuracy of the signal generator used). Sure enough, a true rms meter reads the signal as 353.53 mV. A less-expensive average-responding meter reads the signal as 351 mV.

Unlike the pure sine wave, the triangle wave in Figure 4 has some higher-frequency energy, so the crest factor of 1.732 comes as no surprise. Dividing the peak value by the crest factor yields an expected rms value of roughly 290 mV. Now, the average-responding meter starts to get into trouble, reading the signal as 276 mV, a 4 percent error compared to the true rms meter's reading of 288.68 mV.

Now let's look at pulse trains, where the crest factor depends on the duty cycle. You can get a close approximation of crest factor with the formula:

$$CF \cong \sqrt{\frac{T}{t}}$$

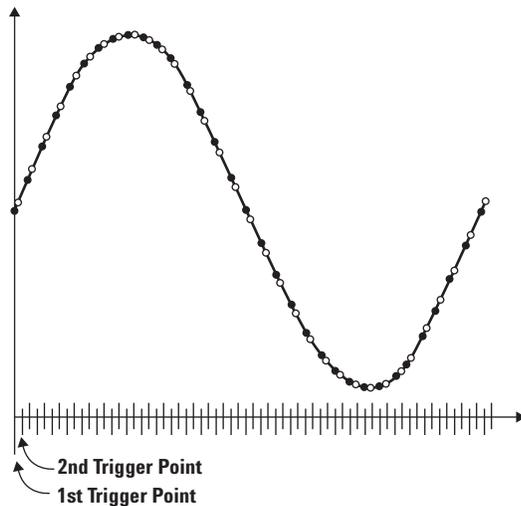
where:

CF = the crest factor

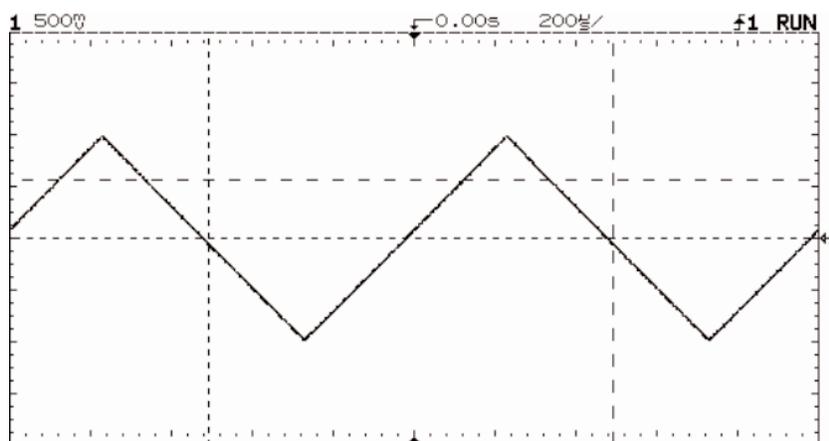
T = the period of the waveform

t = the on portion of that period

**Figure 3.**  
**Digital sampling**



**Figure 4. Measuring rms on a triangle wave**



This also is equal to the square root of the reciprocal of the duty cycle. So, for the pulse train in Figure 5, which has a 2 percent duty cycle, the crest factor is the square root of 50, or 7.071.

Computing the rms value for sines and triangles is quite simple; the rms value is  $V_{pk}$  divided by the crest factor. However, computing the ac rms value for a pulse train is a bit more complicated:

$$V_{rms} = \frac{V_{pk}}{CF} \times \sqrt{\left(1 - \frac{1}{CF}\right)^2}$$

Using the formula, the theoretical rms value of our  $2 \cdot V_{pk}$  pulse train with 2 percent duty cycle in Figure 5 is roughly 280 mV. Even in this case, which is outside its specified performance range, the true rms meter reads 275.9 mV. On the other hand, the average-responding meter reads 73 mV, a 74 percent error. This is an extreme example, but it provides a clear picture of what high crest factors can do to your measurements.

Let's consider one more waveform—the noisy, messy sine wave shown in Figure 6. The true rms meter pegs it at 348.99 mV, which is close to the digital scope's measurement of 345 mV. The average-responding meter puts the value at 273 mV, an error of more than 20 percent. This error is due to the limited bandwidth of the average-responding meter. The signal contains high-frequency energy that the average-responding meter does not take into account.

Figure 5. Measuring rms on a low-duty-cycle pulse train

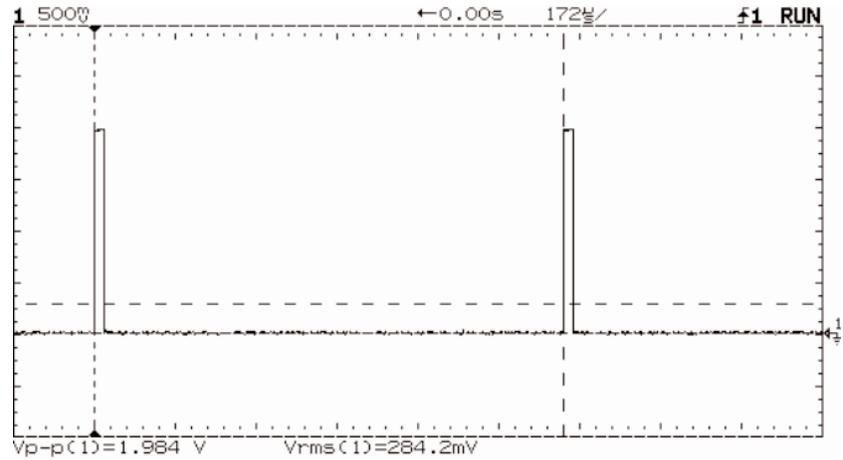
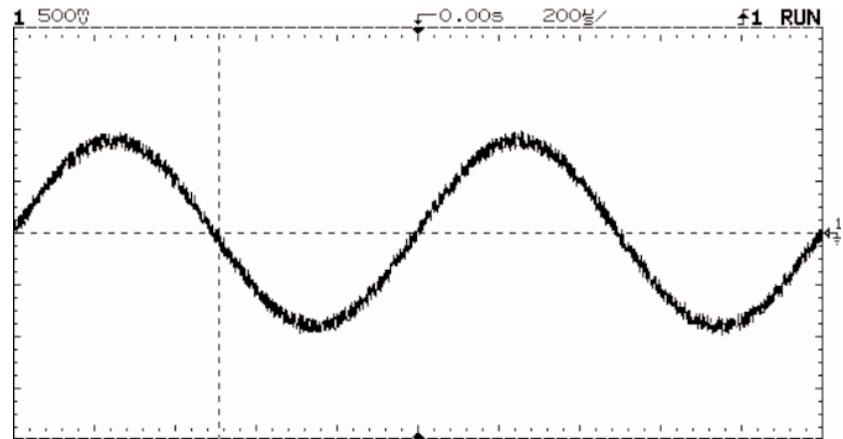


Figure 6. Measuring rms on a noisy sine wave



## Conclusion

### **Tip 3:** **Avoid common measurement traps.**

If an ac rms reading does not make sense, do not automatically assume there is something wrong with your circuit—the trouble might be in how you made the measurement. Below is a list of common traps that can affect rms measurements. We have touched on some of these already, and you may have run into many of them before.

**Measurements below full scale** — Most meters specify ac inputs down to 5 percent or 10 percent of full scale (some go as low as 1 percent of full scale). For maximum accuracy, measure as close to full scale as you can. You might need to override autoscaling in some cases, if a manual setting will help maximize the input range.

**Ac and dc coupling** — It is easy to overlook this simple issue when you are in a hurry. If your meter is ac coupled (or has selectable ac coupling), it inserts a capacitor in series with the input signal that blocks the dc component in your signal. This may or may not be desirable, depending on the signal and what you are trying to accomplish.

If you are expecting to include the dc component, but the meter is ac coupled, the results can be dramatically wrong. As a side note, if you need to measure a small ac signal riding on a large dc offset but your meter doesn't provide ac + dc directly, you can measure the ac component using ac coupling and measure the dc component separately. Then add the two using rms addition:

$$AC + DC = \sqrt{(AC_{rms})^2 + DC^2}$$

**Saturation problems with high-crest-factor signals** — In addition to the problems they cause with high-frequency content, high-crest-factor signals also can wreak havoc on your input range. Think back to that pulse train with a 2 percent duty cycle. Its 7+ crest factor means that the peak value is more than seven times greater than the rms value. That means your meter needs to provide adequate amplitude resolution for the low rms value without saturating on the high peak value.

To make matters worse, you generally do not get an overload indication with crest-factor saturation, either. It is important to check your meter's specifications for maximum crest factor and to refrain from exceeding them.

**Bandwidth errors** — Signals that are rich in harmonics can produce low-reading measurements if the more significant of these components are not included in the measurement. Check the instrument's data sheet to see how much bandwidth you have to work with. Then make sure your signals do not exceed it.

**Self-heating errors** — High voltages can heat up the meter's signal-conditioning components, leading to offset measurement values. Pay attention to the maximum input voltage; if you exceed it, give the meter time to cool down before making another measurement.

**Settling time** — By definition, rms measurements require time averaging over multiple periods of the lowest frequency being measured. Consequently, if you are not concerned about low frequencies in a particular measurement and your DMM has selectable averaging filters, switch to a faster filter.

While ac rms measurements are more complicated than they might seem at first glance, a little bit of knowledge can help you deal with the complexity. If you have not already done so, verify the crest factor, bandwidth, and other limitations noted in your DMM's data sheet. As much as possible, stay within those limits.

A quality meter used within its limits should deliver consistently dependable measurements.

## Glossary

*Crest factor*—a measure of how high the waveform peaks, relative to its rms value

*DMM*—digital multimeter

*rms* — an abbreviation for root-mean-square

*True rms*—The term “true” rms is used to distinguish meters that actually measure the rms value, from meters that derive rms levels from either peak or average values

$V_{avg}$ —average voltage, using the absolute value of the waveform (the negative portion of the cycle is treated as if it were positive)

$V_{pk}$ —peak voltage

$V_{pk-pk}$ —peak-to-peak voltage

$V_{rms}$ —the rms value of ac voltage

## Related Agilent literature

Data sheet—Agilent 34401A Multimeter,  
pub. no. 5968-0162EN

Data sheet—Agilent 3458A Multimeter,  
pub. no. 5965-4971E

Product overview—Agilent 34970A  
Data Acquisition/Switch Unit,  
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