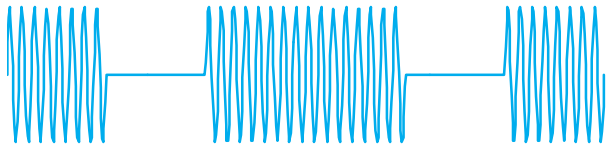


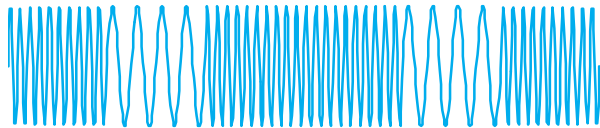
# **EE303 Lesson 20: Digital Modulation 2**

# Digital modulation schemes

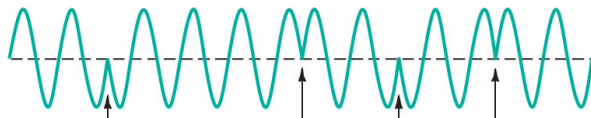
- We've discussed these types of digital modulation



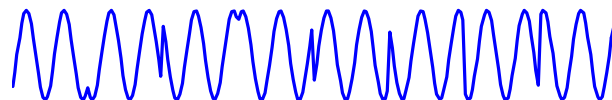
**OOK signal**



**FSK signal**



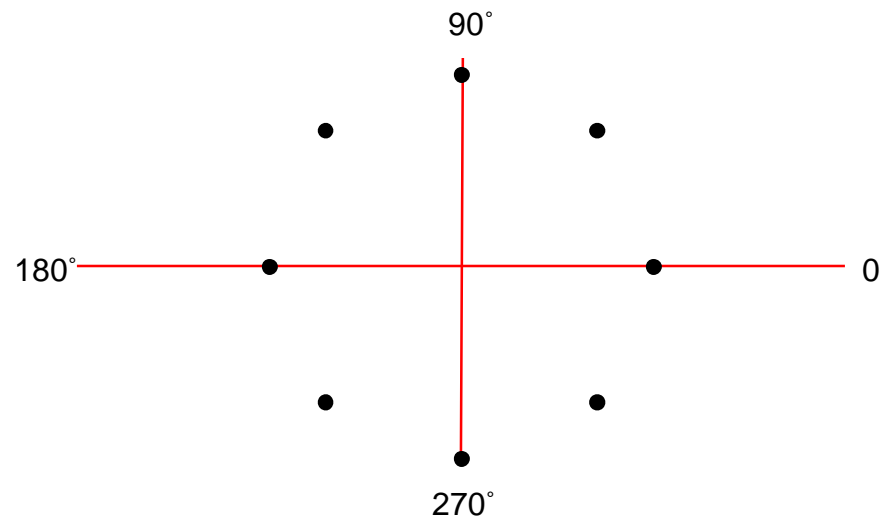
**BPSK signal**



**QPSK signal**

# M-ary PSK

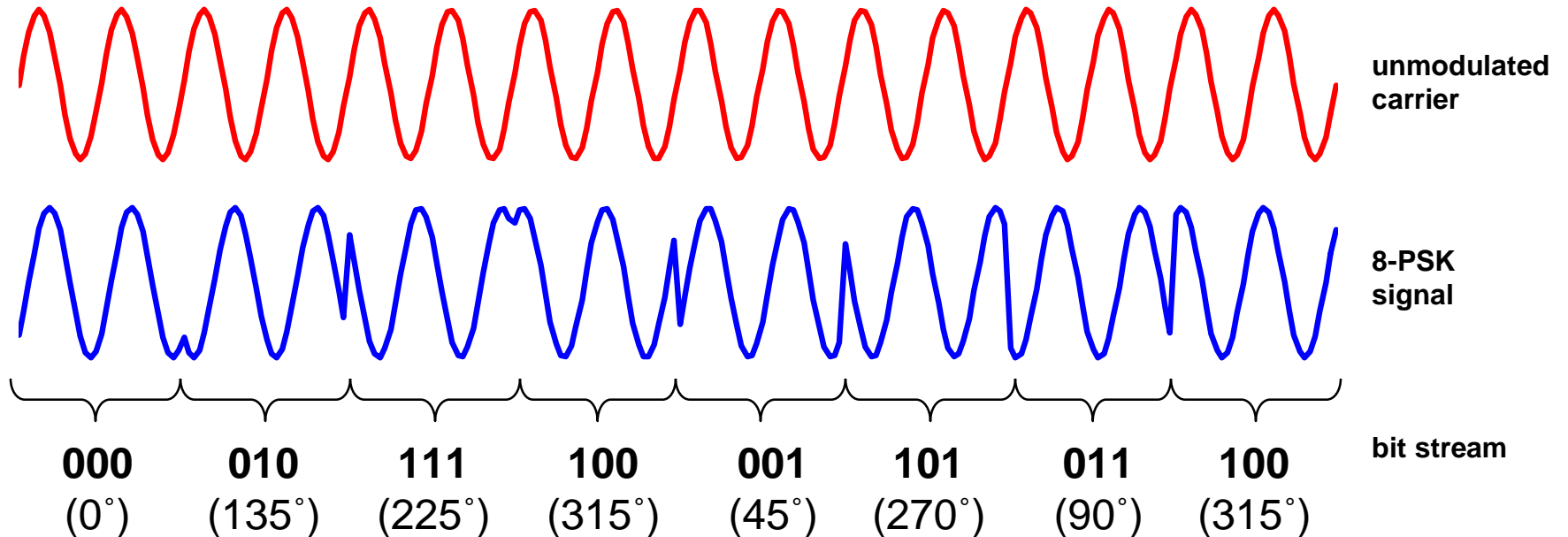
- In order to increase the data rate without increasing bandwidth, we can further increase the number of bits per symbol.
- In the 8-PSK constellation below, 8 possible phase shifts allow 3 bits to be transmitted by each symbol.



0° = binary 000  
45° = binary 001  
90° = binary 011  
135° = binary 010  
180° = binary 110  
225° = binary 111  
270° = binary 101  
315° = binary 100

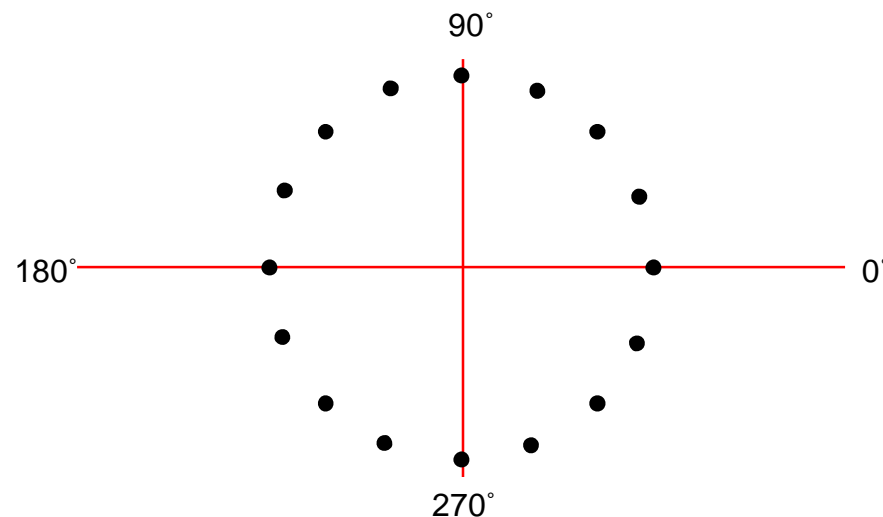
# 8-PSK

- Consider the bit stream below and the resulting 8-PSK signal.



# 16-PSK

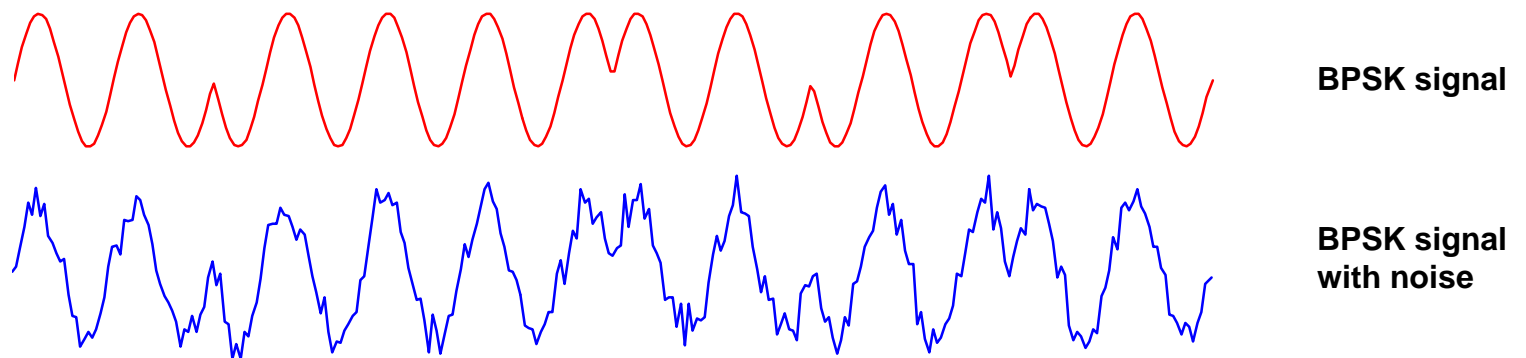
- We could further increase to 4 bits/symbol using 16-PSK.



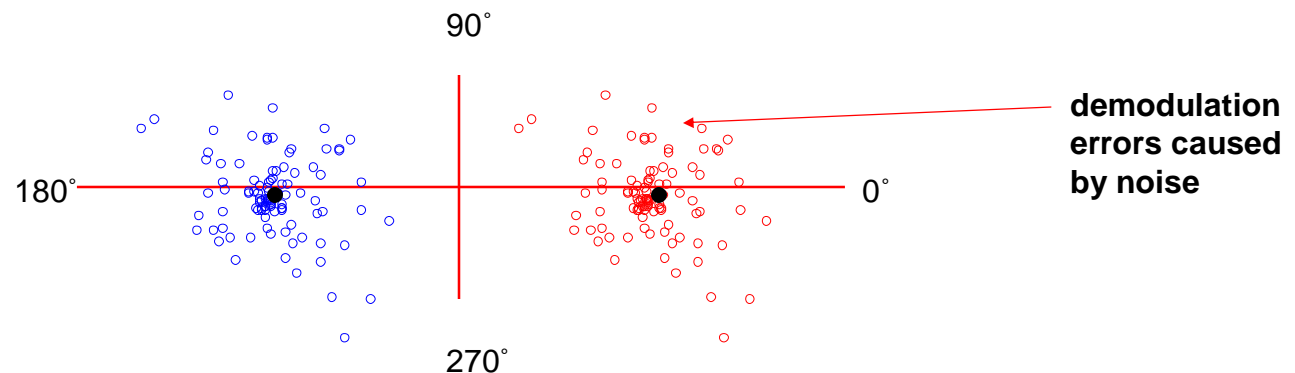
- To demodulate 16-PSK, the receiver must determine the phase within  $\pm 11.25^\circ$ .

# Noise effects

- Like all transmissions, the received signal will be degraded by noise.

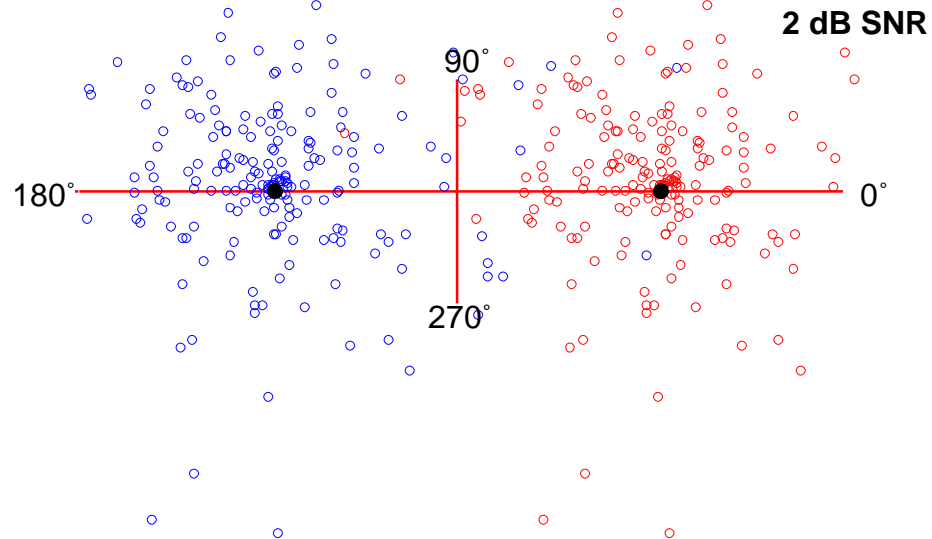
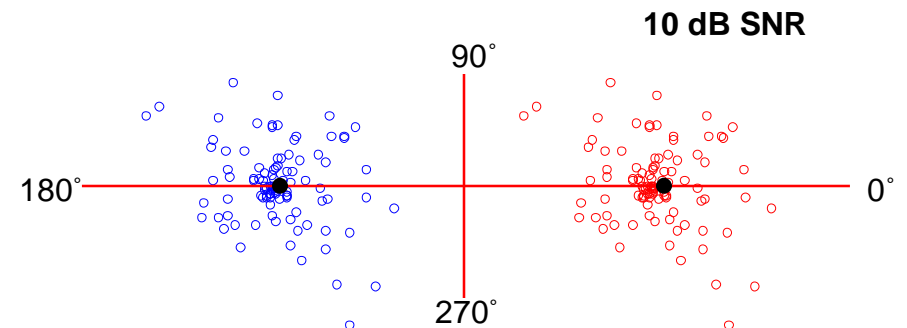
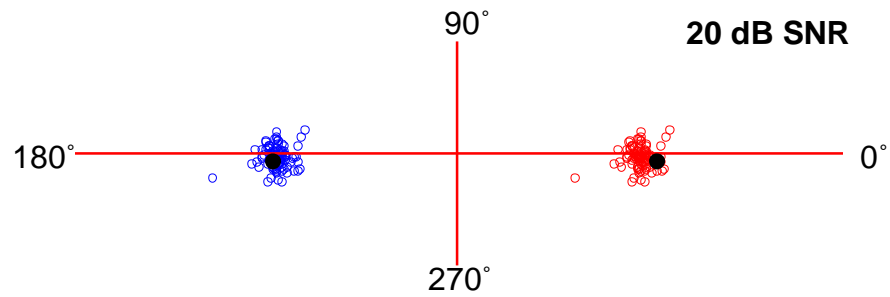


- This can be depicted in the phasor domain as follows.





# Noise effects



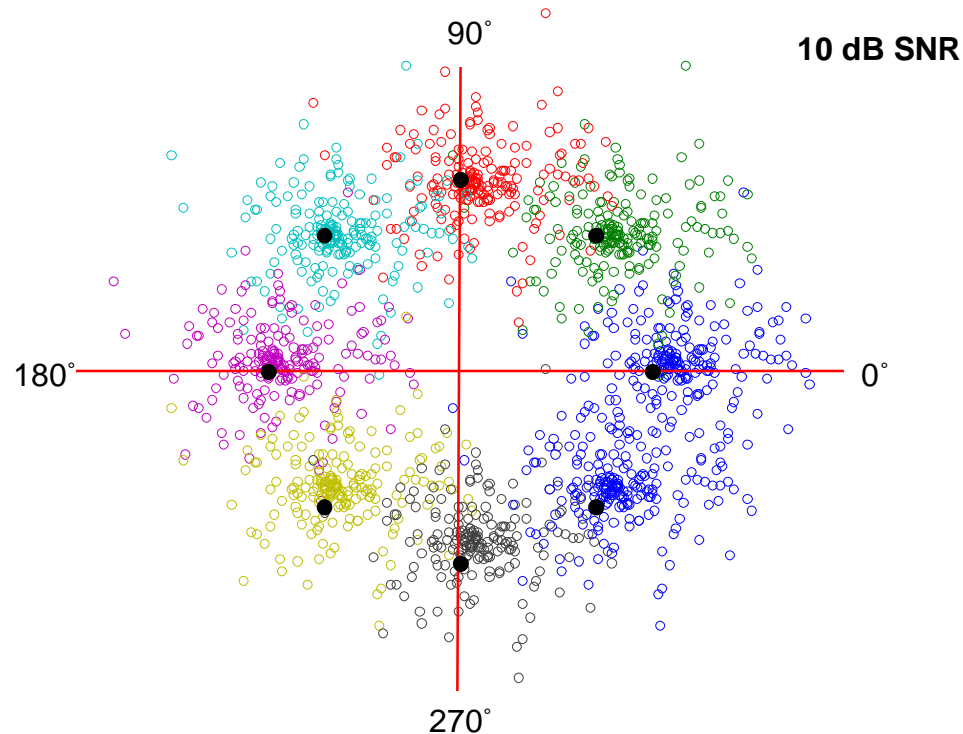


# Noise effects

- A BPSK receiver must make a decision to determine the phase of a received signal to determine the corresponding binary signal.
- Now consider the same noise in the presence of a QPSK or 8-PSK signal.



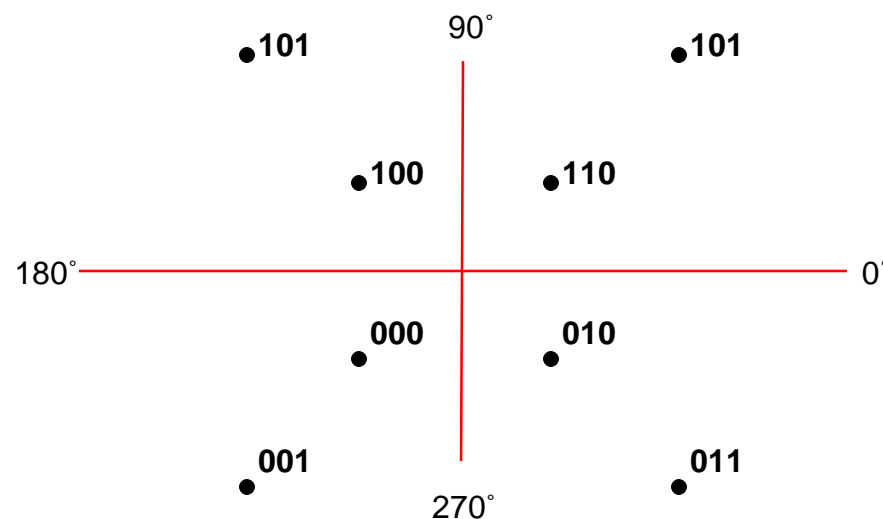
# Noise effects (8-PSK)



- What is the relative likelihood of an error?

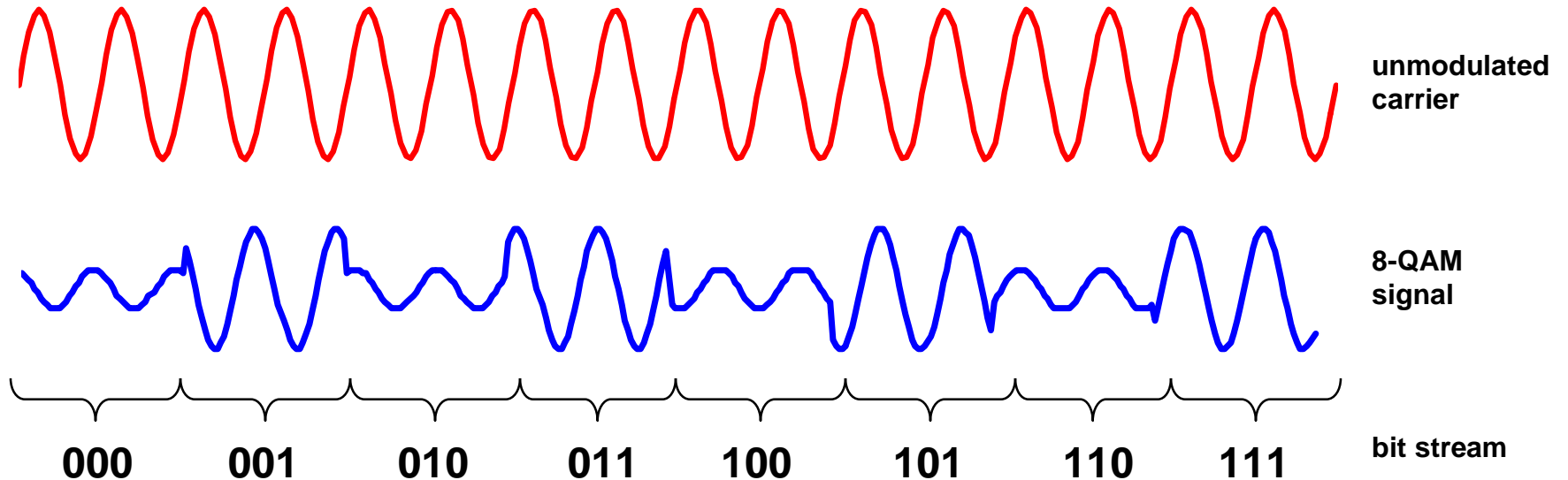
# Quadrature Amplitude Modulation

- In order to increase the distance between points in the signal constellation, another option is to modulate both the amplitude and the phase.
- This is called quadrature amplitude modulation.
- Consider the 8-QAM constellation below.



# 8-QAM

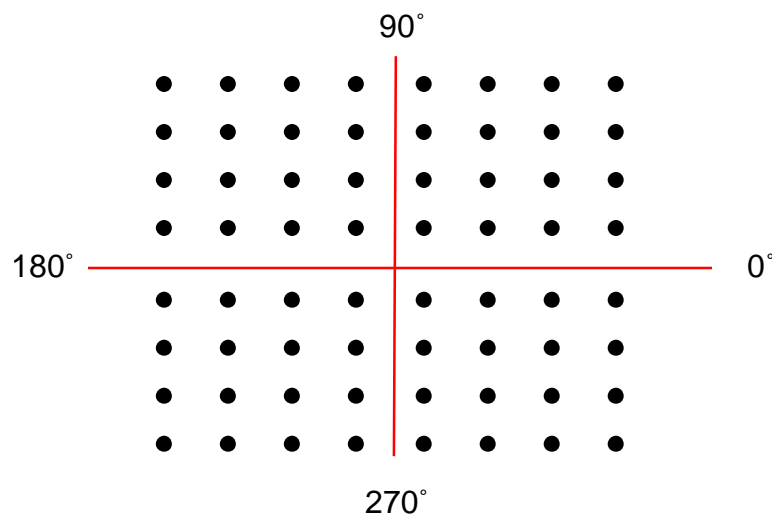
- Consider the bit stream below and the resulting 8-QAM signal.



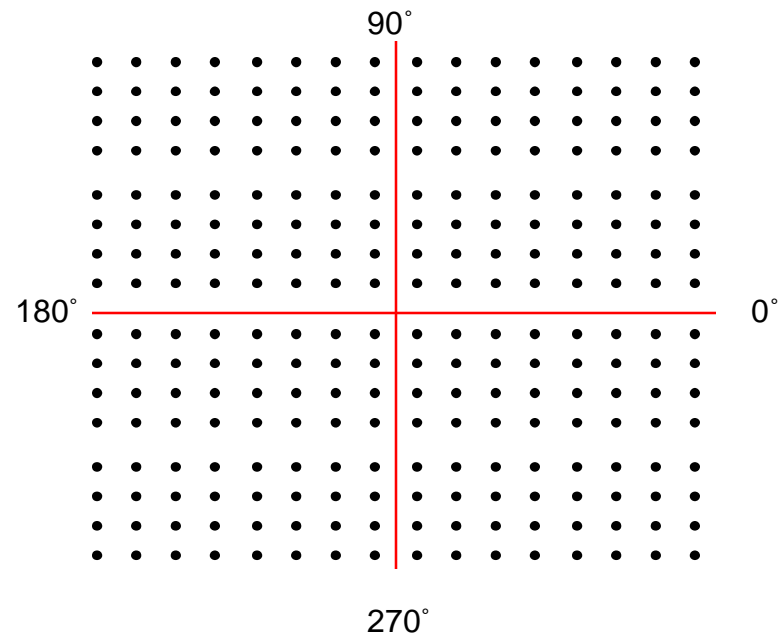
# Higher level QAM signals

- QAM signals can be extended to much higher bit rates as depicted.
- 64-QAM and 256-QAM are common in cable modems, satellites, and high-speed fixed broadband wireless.

**64-QAM**



**256-QAM**





# Spectral Efficiency

- Spectral efficiency is a measure of how fast data can be transmitted over a given bandwidth.
- It is measured in bits per second per hertz (bps/Hz).

Modulation	Spectral efficiency (bps/Hz)
FSK	<1
MSK	1.35
BPSK	1
QPSK	2
8-PSK	3
16-QAM	4



## Example Problem 1

Based on the spectral efficiency of the various digital modulation schemes, what is the minimum bandwidth required to transmit at a rate of 9600 bps using:

- a. MSK (or GMSK)
- b. BPSK
- c. 8-PSK
- d. 16-QAM

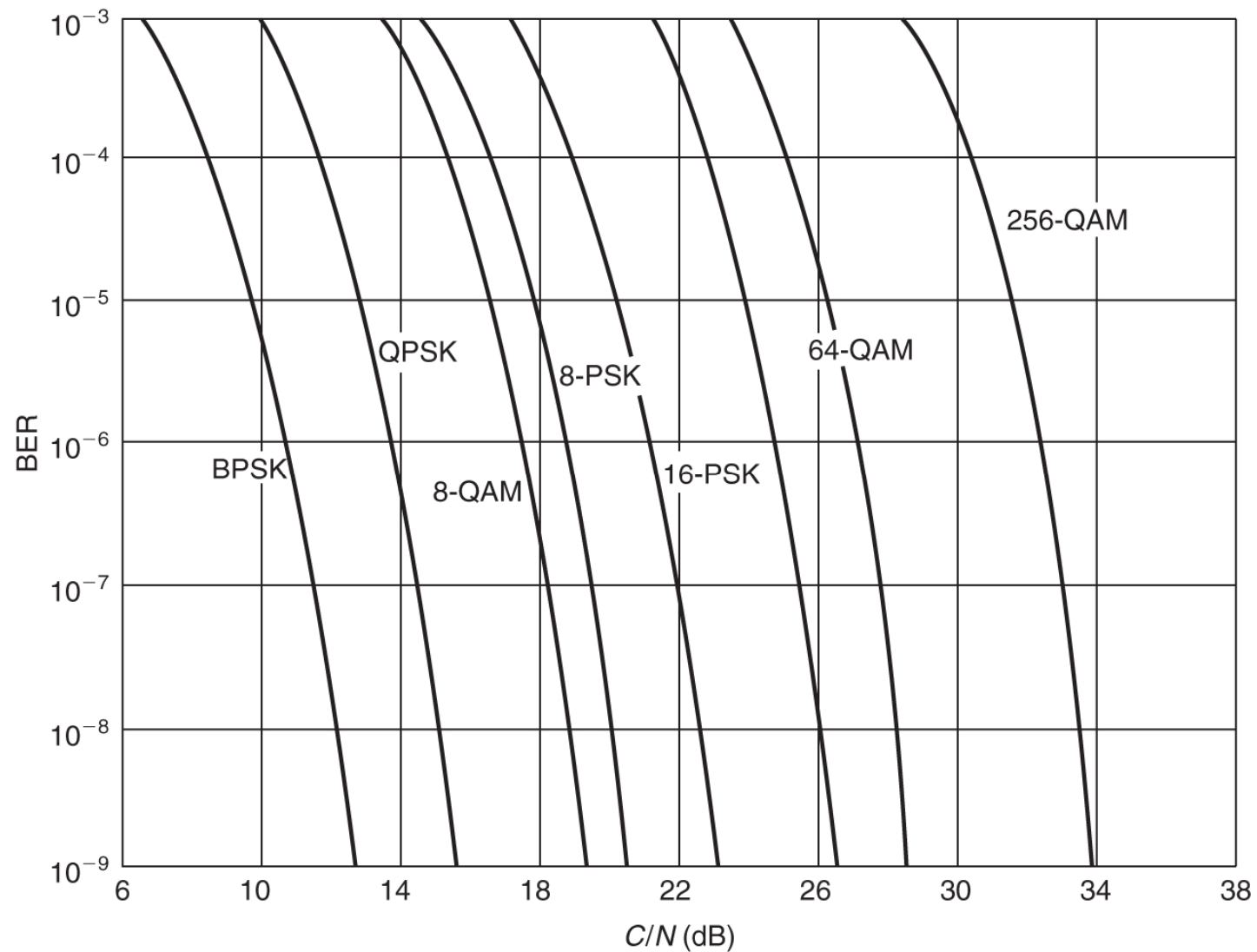


# Bit errors

- Another factor that influences spectral efficiency is channel signal-to-noise (S/N) ratio.
- The larger the amount noise present (lower S/N ratio), the greater the number of bit errors.
- The ratio of the number of bit errors to the number of bits transmitted is the bit error rate (BER).
- For example, if 5 bit errors occur every million transmitted bits, the BER is

$$BER = \frac{\text{number of errors}}{\text{number of transmitted bits}} = \frac{5}{1,000,000} = 5 \times 10^{-6}$$

# BER vs. $C/N$ for digital modulation







# BER vs. $C/N$ for digital modulation

- The bit error rates of various modulation schemes have been calculated versus carrier signal-to-noise ratios.
- The plot shows that the more basic modulation schemes (BPSK, QPSK) have a higher immunity to noise than the more complex constellations.
- This plot does not take signal bandwidth into consideration (noise increases with bandwidth)
- Also, the plot does not take into account the bit rates of the various formats.



## Example Problem 2

What is the required carrier signal-to-noise ( $C/N$ ) ratio required to achieve a BER of  $10^{-6}$  for each of the following modulation schemes?

- a. BPSK
- b. QPSK
- c. 16-PSK
- d. 256-QAM



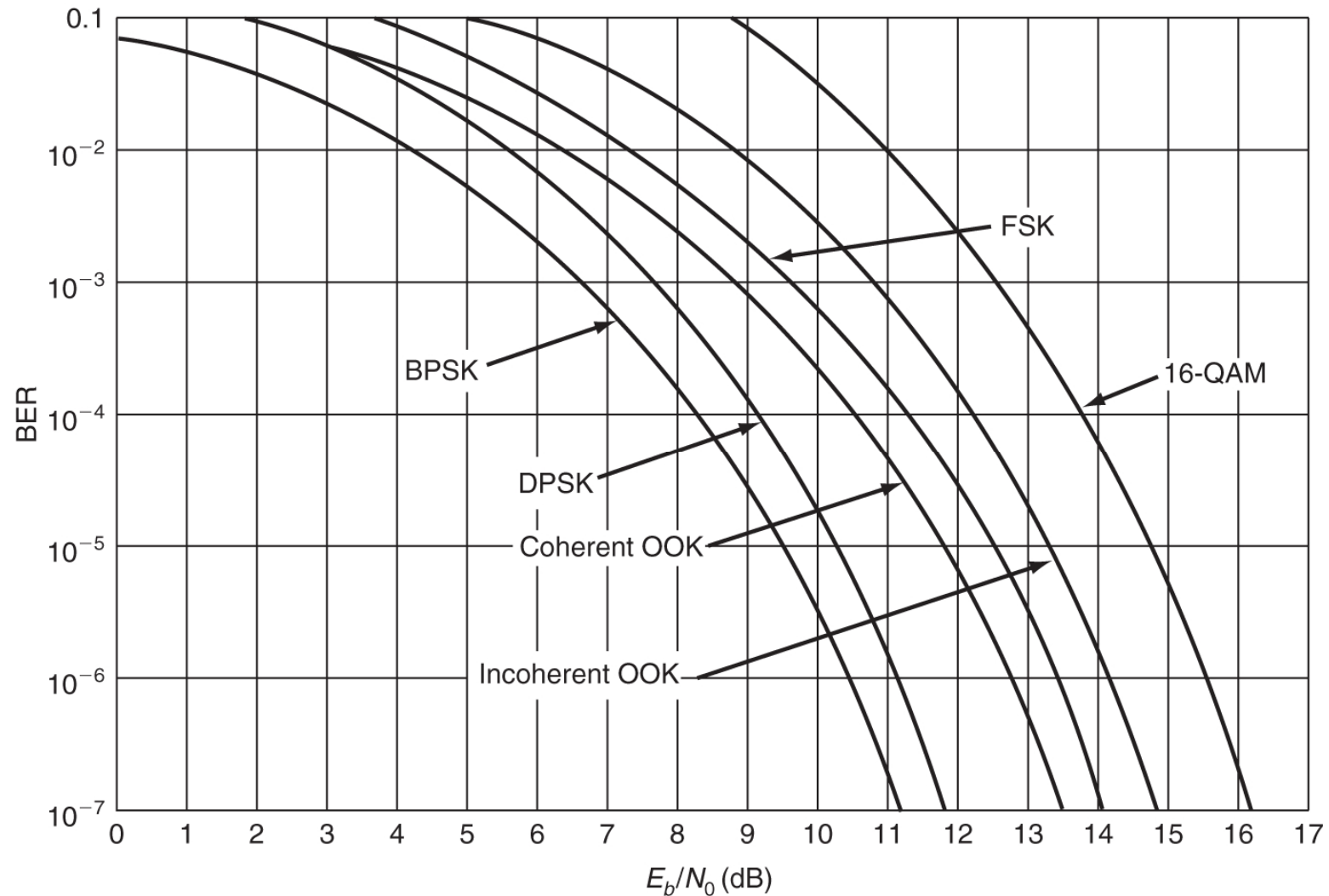
$$E_b/N_0$$

- A better measure of signal to noise ratio is to compare the energy per bit ( $E_b$ ) versus the noise power density ( $N_0$ ) given by

$$\frac{E_b}{N_0} = \left( \frac{C}{N} \right) \left( \frac{B}{f_b} \right)$$

- $E_b/N_0$  takes into account the bandwidth requirements and bit rates of the various formats.

# BER vs. $E_b/N_0$ for digital modulation





## Example Problem 3

Consider transmitting 10,000,000 bits over a channel with a S/N ratio (expressed in  $E_b/N_0$ ) of 10 dB. Roughly how many bits errors would you expect to experience for each of the following modulation schemes?

- a. BPSK
- b. Coherent OOK
- c. FSK
- d. 16-QAM