

# Capacitive sensors and their readout electronics

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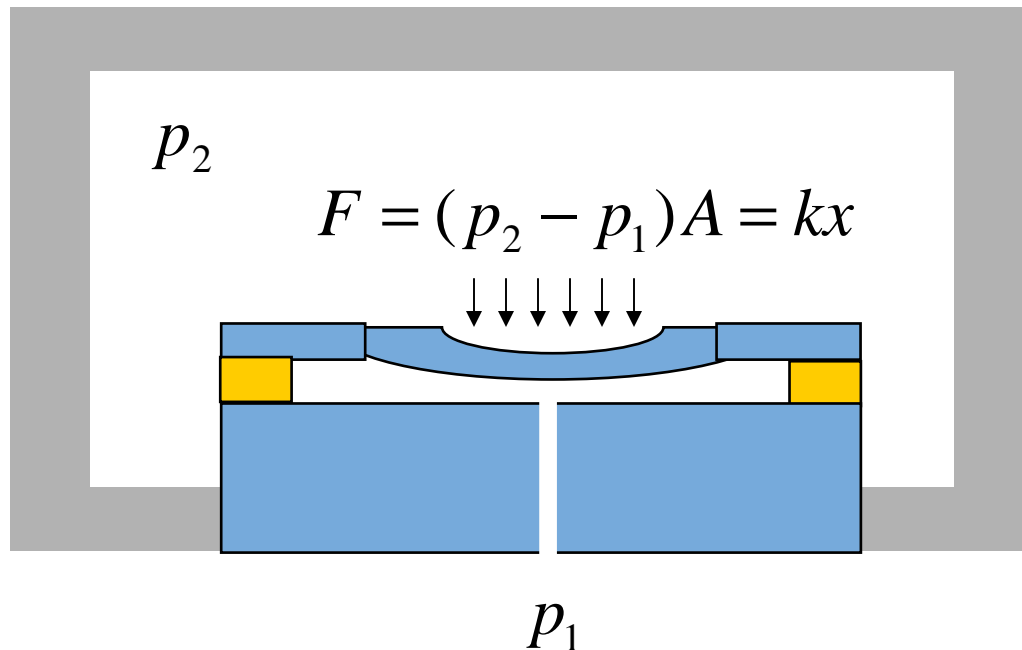
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## Motivation for capacitive sensors

- Low power consumption
- High resolution
- Small temperature coefficient (e.g., in capacitive MEMS sensors)
- Possibility for high-volume manufacturing (e.g., by using MEMS technology)
- Potential for low cost
- Potential for monolithic integration with readout electronics
- Possibility to reuse of IP blocks (i.e., designs) both in IC and MEMS parts
- In capacitive MEMS sensors, the dynamic range can be tailored in a wide range by scaling the dimensions of the MEMS structure

## Example: Capacitive pressure sensor



$$x = \frac{3(1-\nu^2)}{16} \frac{\Delta p R^4}{Et^3}$$

$$x < t$$

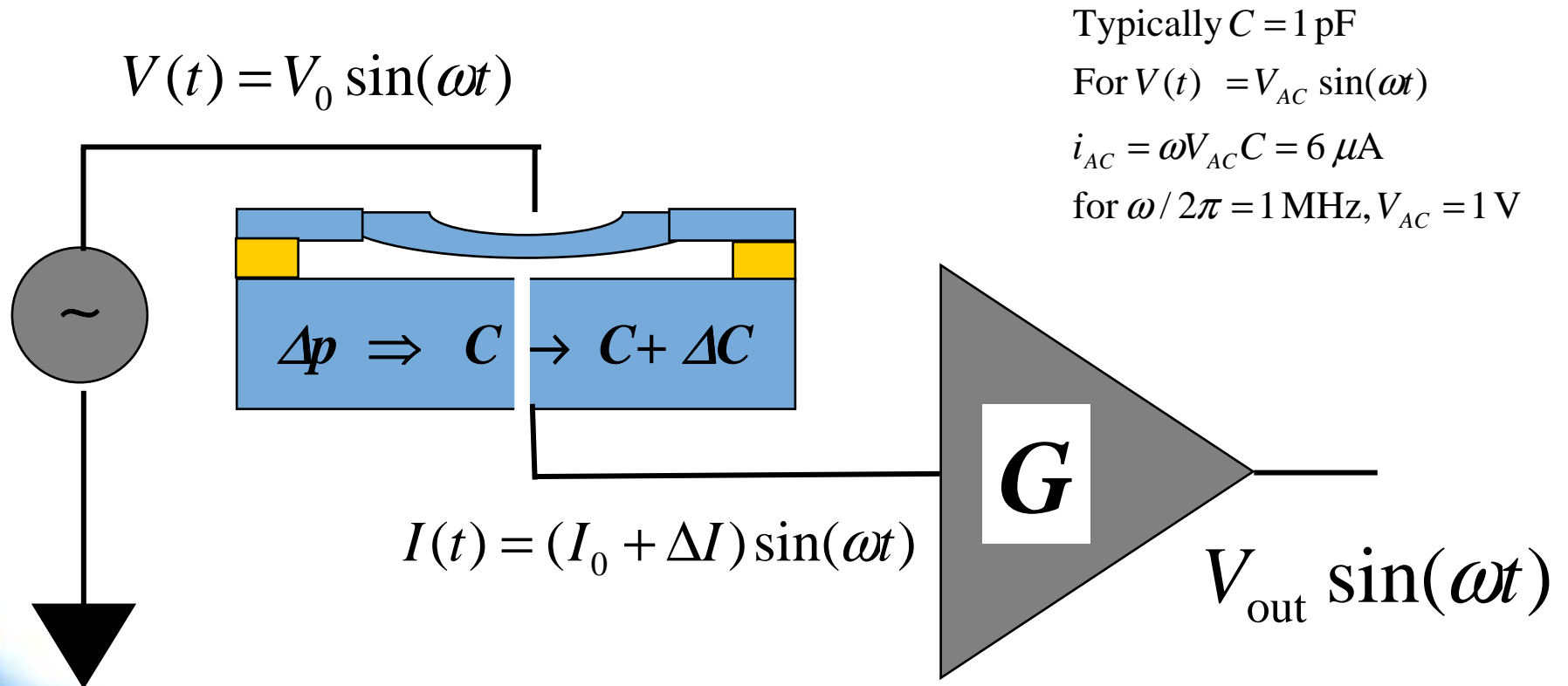
$$\Delta p_{\max} = \frac{16}{3(1-\nu^2)} \frac{Et^3 d}{R^4}$$

“Convenient” measuring range (*dynamic range*) for a Si sensor with the area  $1 \text{ mm}^2$  is  $p = 0.01 \text{ bar} \dots 100 \text{ bar}$

Dynamic range limited by nonlinearity and eventually the membrane touching the bottom wafer (=> advantage: tolerance against pressure shocks)

## Readout of a capacitive sensor

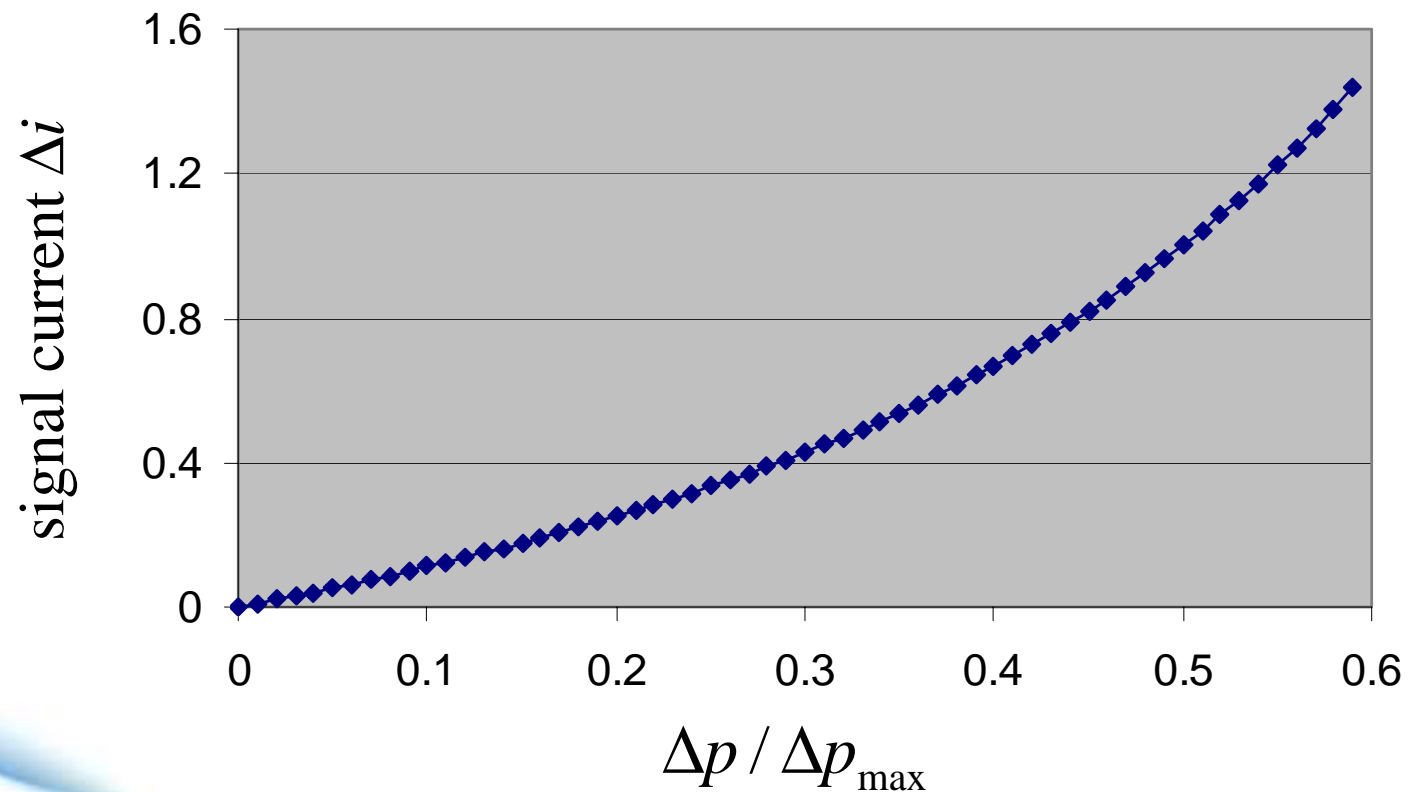
### 1. AC readout (i.e., displacement measurement)



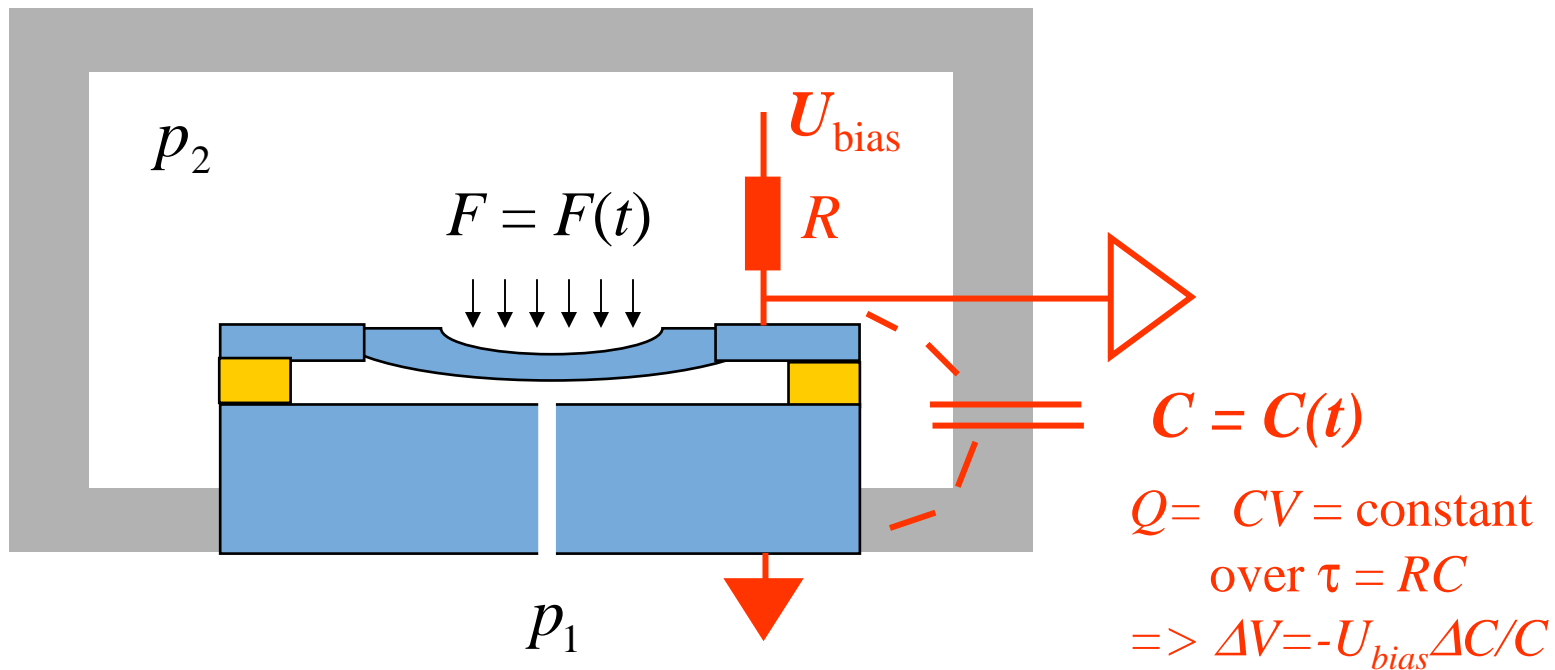
## Transfer function of the capacitive pressure sensor

$$\Delta i = \omega \Delta C U_{AC}$$

$$C \approx \frac{C_0}{1 - x/d}$$



## 2. DC readout (velocity measurement)



**Bias the membrane by “constant” charge and measure voltage changes induced by the motion of the membrane**

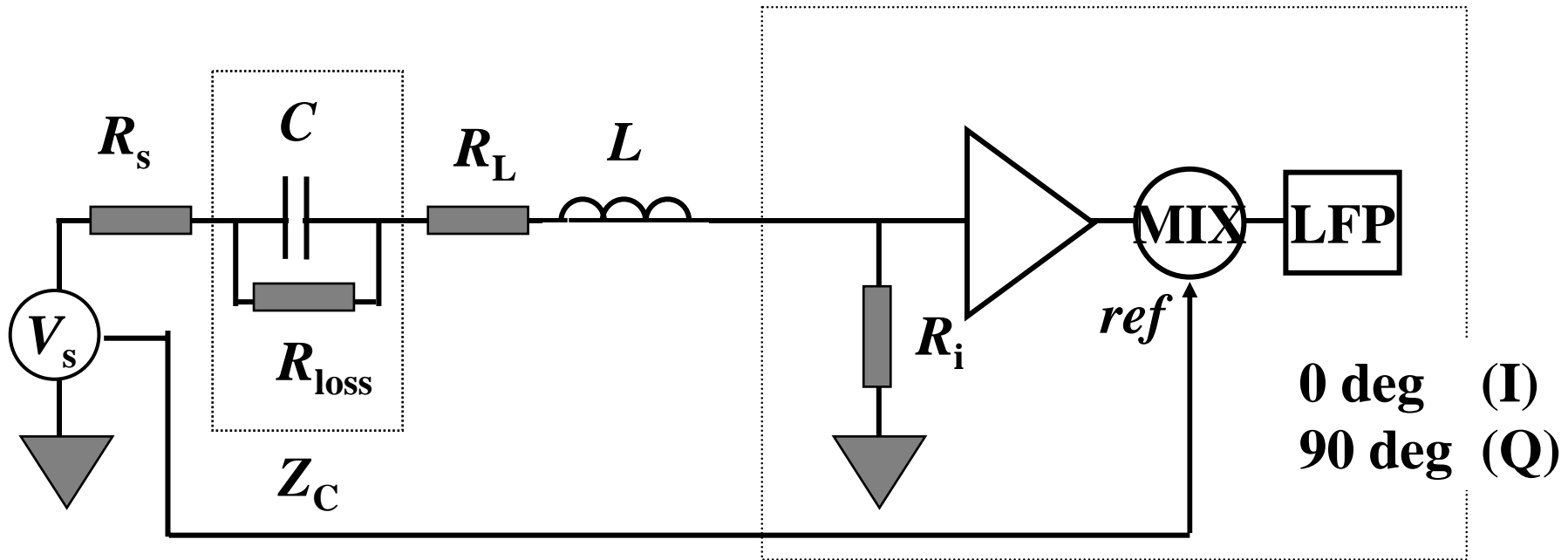
Velocity of the diaphragm is measured, NOT position

Motional current (calculate typical example)

Examples: microphone, dynamical pressure, vibration, resonators

### 3. Readout using a tuned circuit

IMPROVED RESOLUTION BY TUNING!



$Q$ -factor enhancement to the 90 deg signal => high resolution

$\text{Sqrt}(Q)$  enhancement of the noise at the resonance frequency

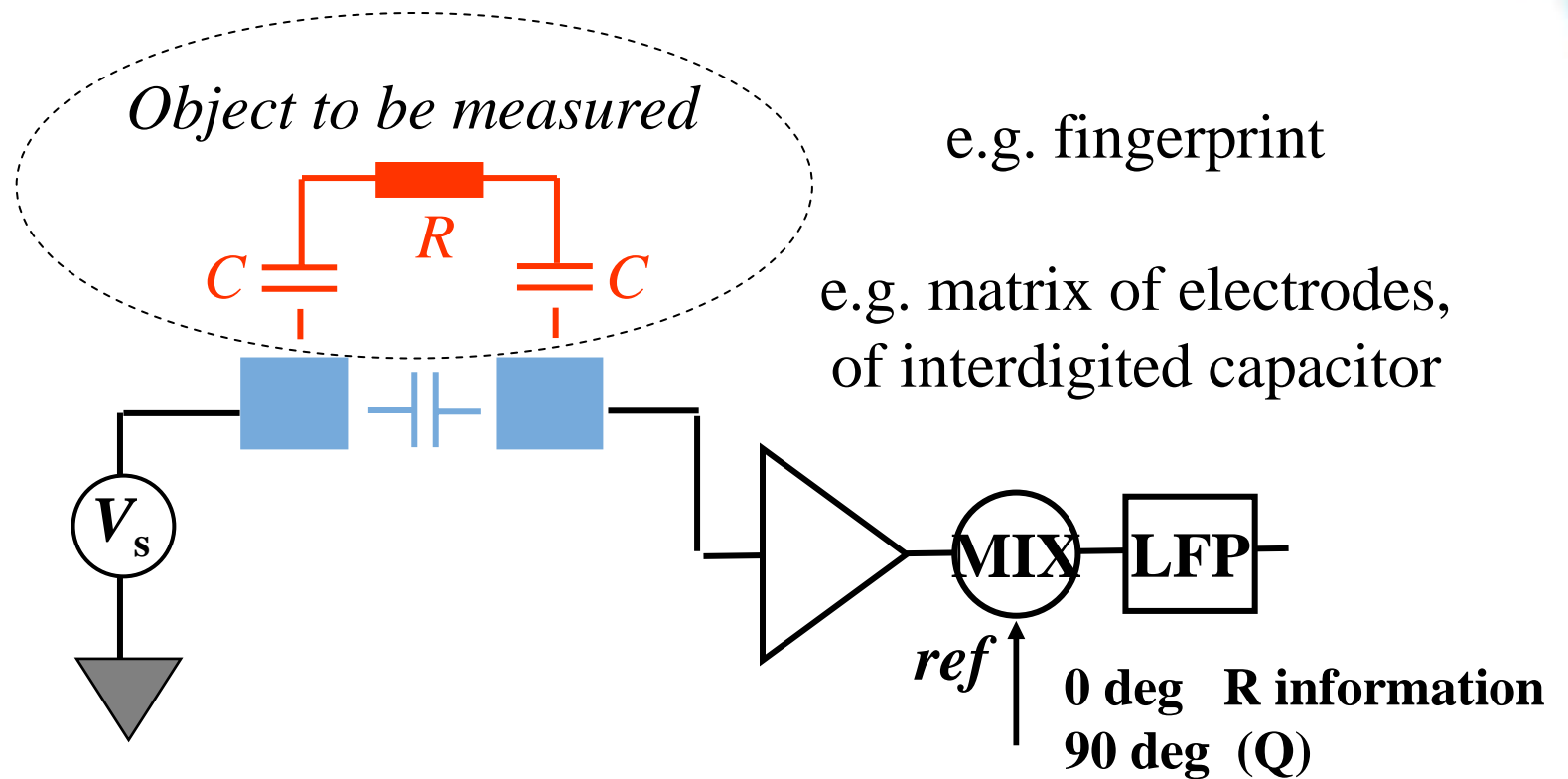
Long term stability of the tuned circuit problematic (e.g., T coeff of the inductor)

0 deg signal is a measure of the loss factors

Suited particularly for dynamic measurements: dynamic pressure, microphone, vibration, ...



#### 4. Capacitive sensors based on the loss factor measurement



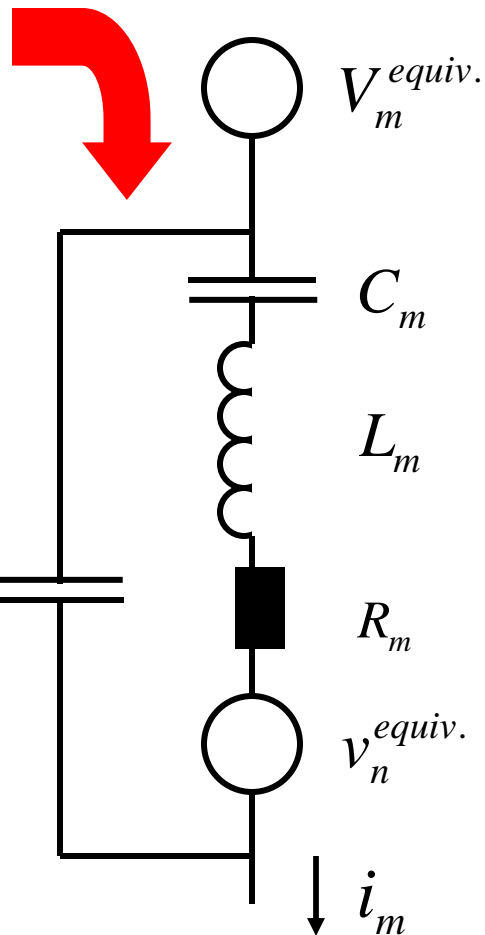
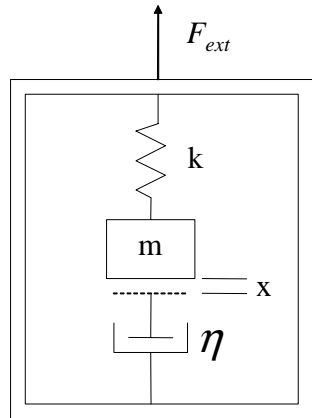
## 5. Resonating capacitive sensors

### Advantages over static capacitive sensors

- Improved resolution (at least sometimes)
- Easier to make a readout electronics which does not limit the resolution
- Output can be coded in the *frequency* of the output voltage. This may be an advantage.
- Several measurements can be measured transformed into a mechanical resonance measurement (strain, force, pressure, acceleration, temperature, mass deposition, ..)
- Additional information can be obtained from the dissipation (Q value of the mechanical resonance)

# Equation for the mechanical resonance

$$m \frac{d^2 x}{dt^2} + \eta \frac{dx}{dt} + kx = F_{ext} \quad F_{ext} = \text{Mechanical force} + \text{Electrical force}$$



Static capacitance  $C_0$

Transfer function at operation point:

$$|G(\omega)| = \frac{1}{\sqrt{(\omega_0^2 - \omega^2)^2 + \frac{\omega_0^2 \omega^2}{Q^2}}}$$

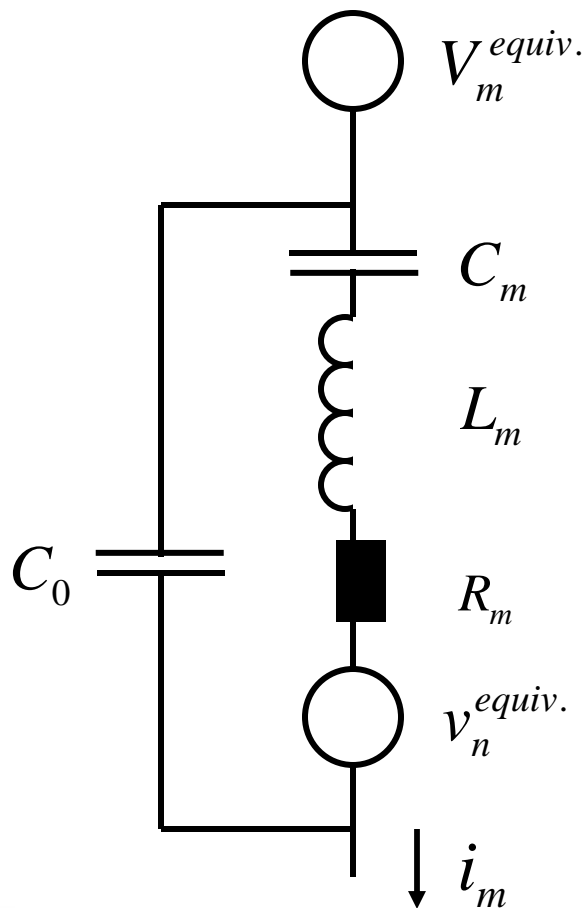
$$\omega_0 = 2\pi f_0$$

$$Q = \omega_0 m / \eta$$

Motional quantities (“m”)

$$v_n^{equiv.} = \sqrt{4k_B T R_m}$$

# Mechanical resonator as a sensor

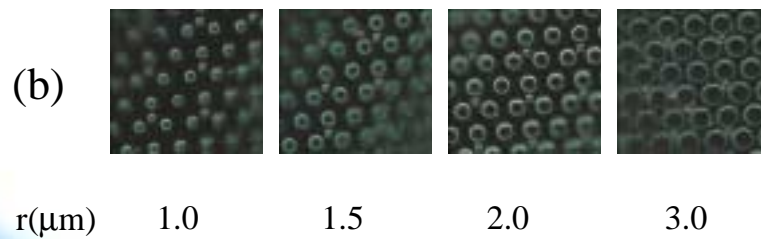
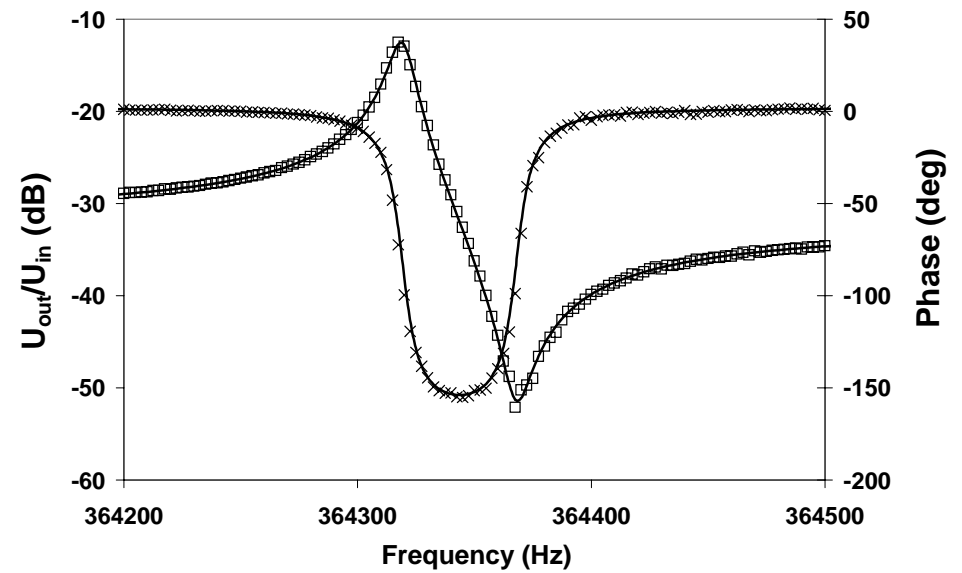
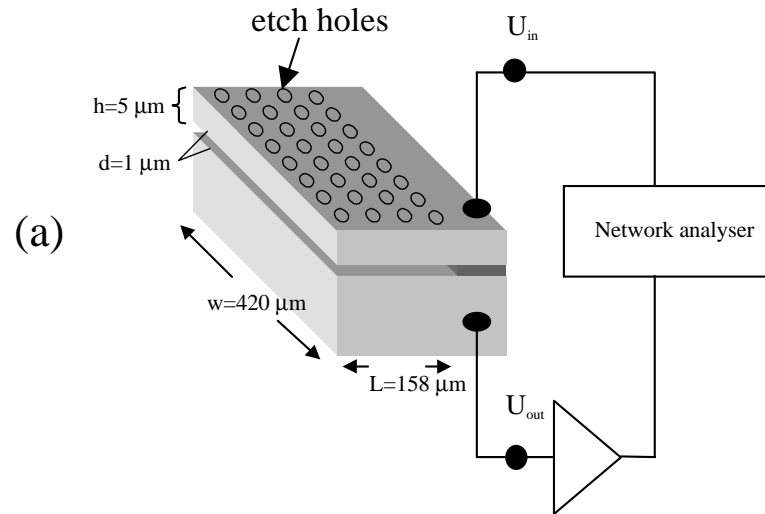


Spring term: strain, force, pressure, acceleration, ..

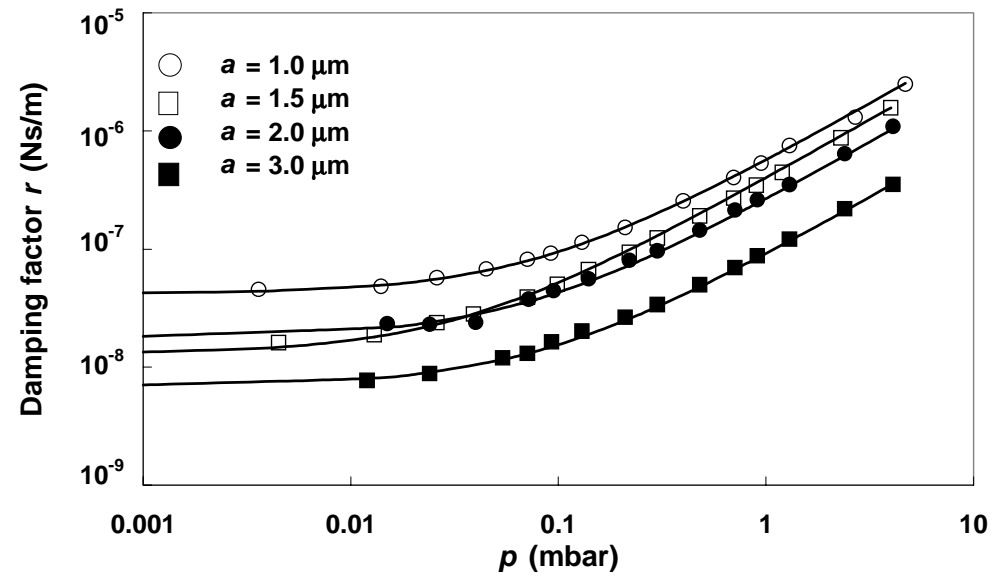
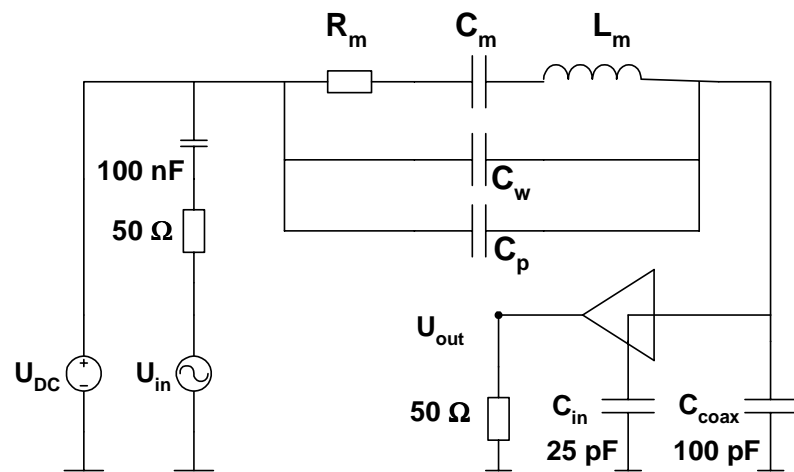
Mass term: mass change, pressure, ..

Loss term: pressure from flow loss, viscous surface effects, rapid mass fluctuations, ...

## Example: resonating pressure sensor (Tomi Mattila et al, 2000)

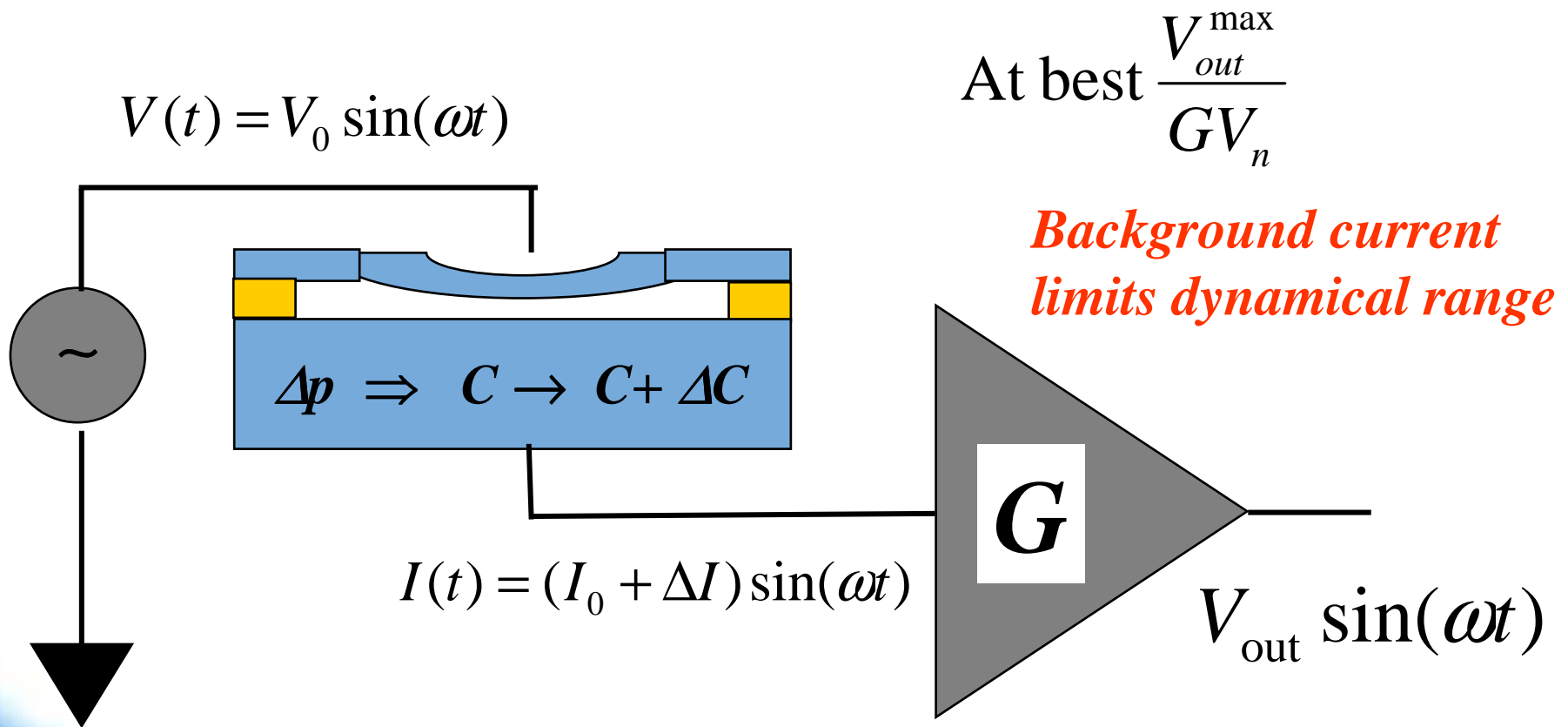


## Example: resonating pressure sensor (2)



## Measurement techniques related to capacitive sensors

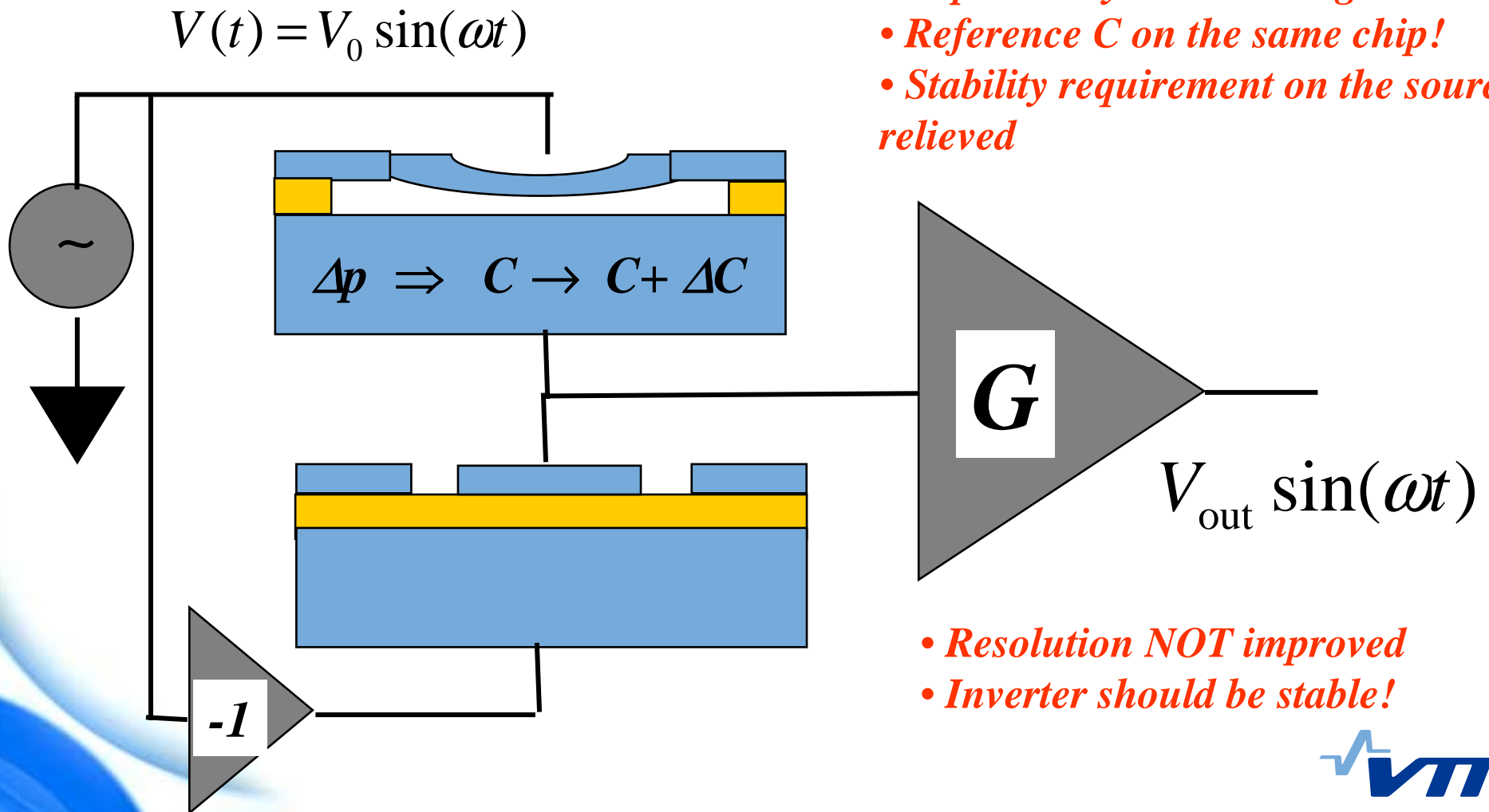
## Dynamical range of AC readout





## Bridge measurement

- *Zero background signal*
- *Improved dynamical range*
- *Reference C on the same chip!*
- *Stability requirement on the source relieved*



- *Resolution NOT improved*
- *Inverter should be stable!*

## Guarding of parasitic capacitances

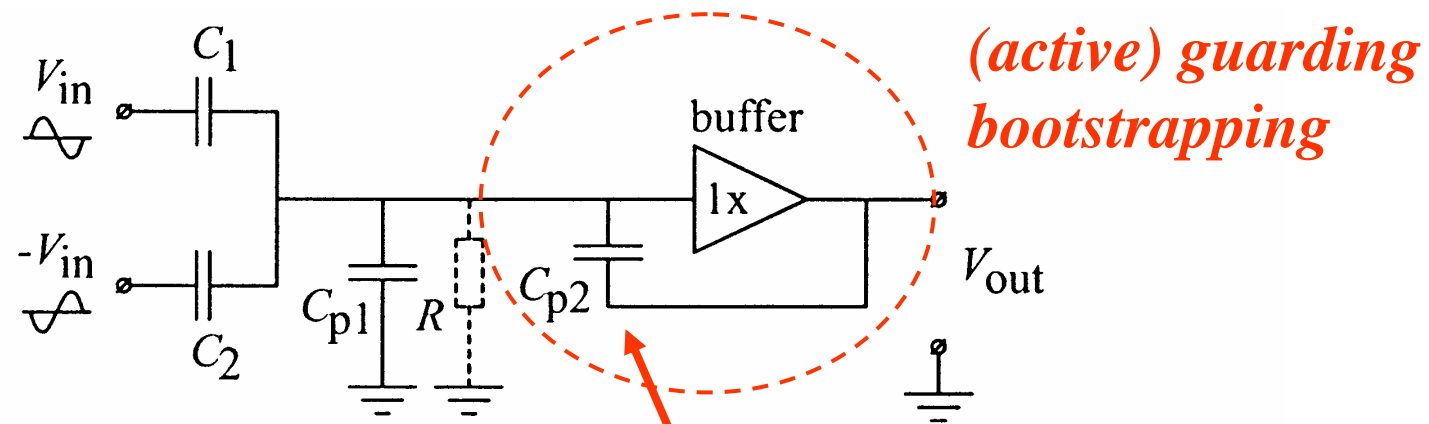


Fig. 10.14. Elimination of parasitic capacitor  $C_{p2}$  by bootstrapping

**Intrinsic parasitic C**  
(cannot be bootstrapped)  
(f.ex. anchor area of  
released MEMS)

**Parasitics from cables, f.ex.**  
(CAN be guarded)

## Guarding of parasitic capacitances (2)

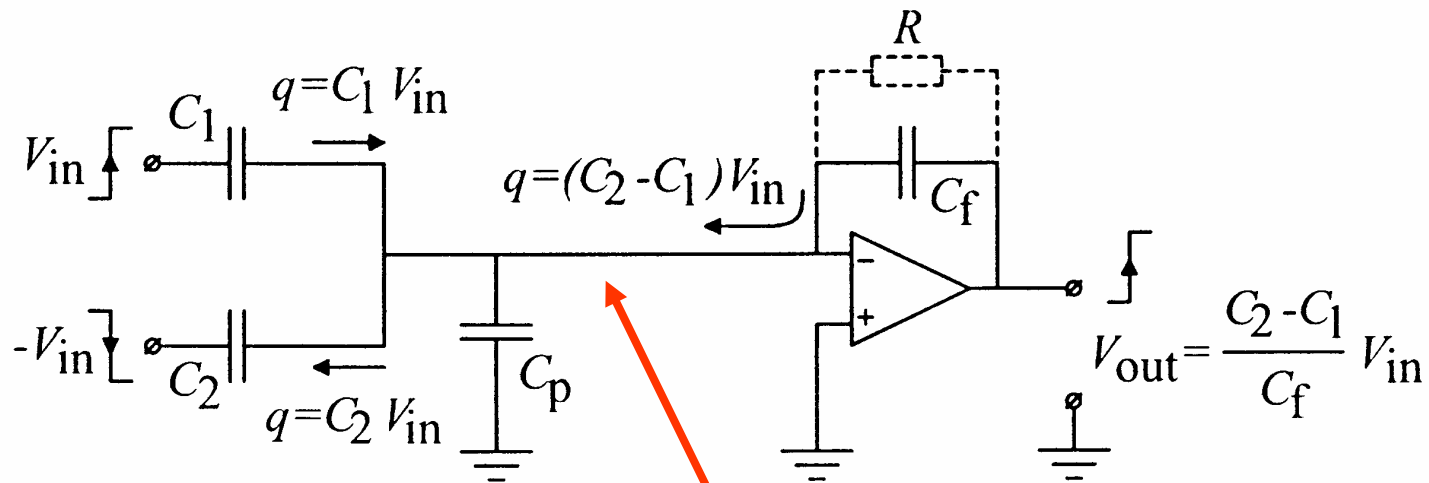


Fig. 10.15. Principle of charge sensing

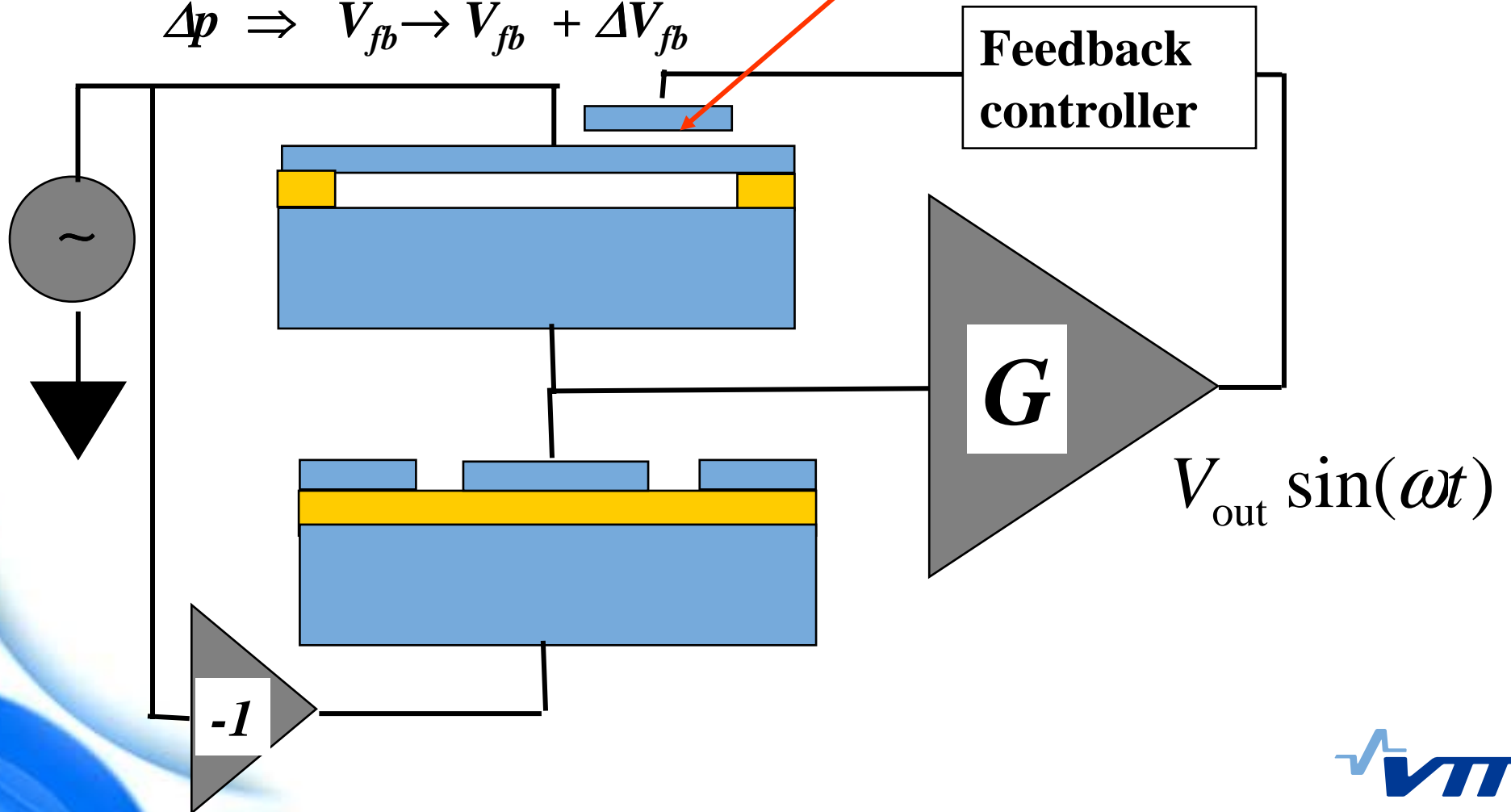
**The potential of the signal line is kept at virtual ground => no current flows across  $C_p$**

## Force feedback

*Electrostatic force*

$$F_e = \frac{\epsilon AV^2}{2d^2}$$

$$\Delta p \Rightarrow V_{fb} \rightarrow V_{fb} + \Delta V_{fb}$$



## Features of force feedback

**Nonlinearity of the spring does not matter since the membrane is not moving**

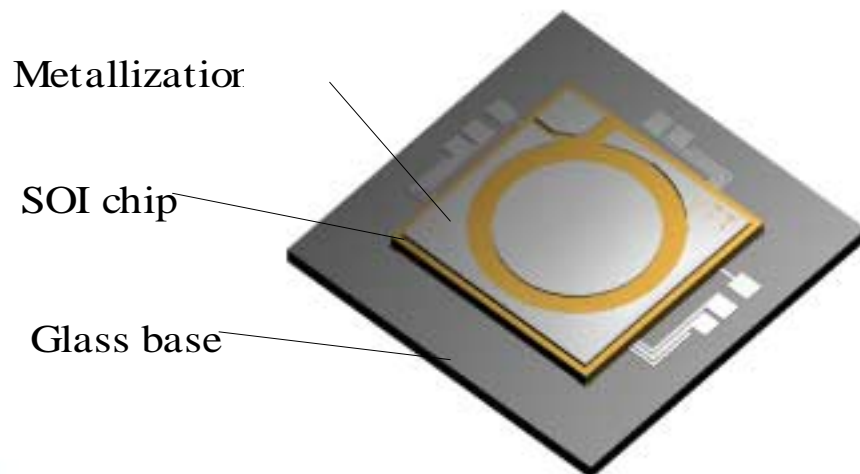
**Linearity requirement now concerns the feedback circuitry, not the transducer**

**Obtaining linearity requires special solutions since electrostatic force is proportional to the voltage squared**

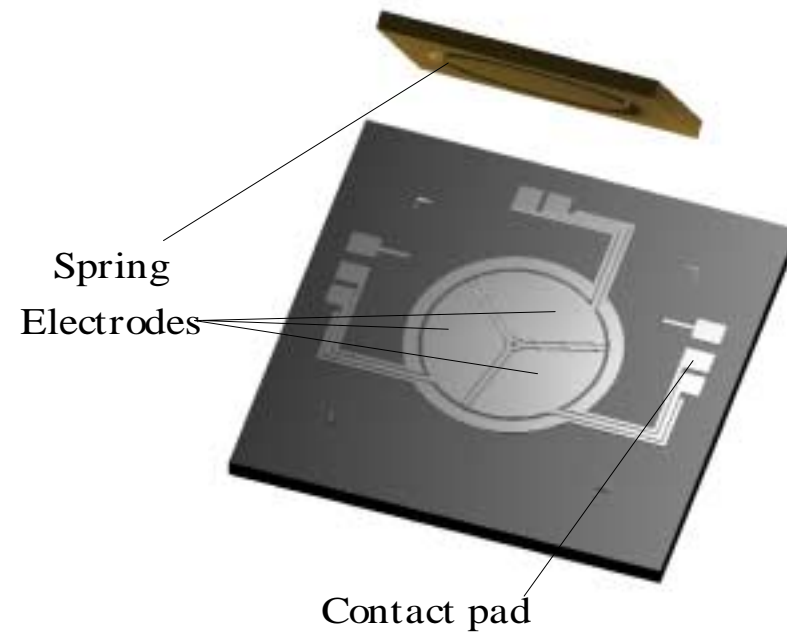
**Transfer function is modified by the feedback**

## Micromechanical silicon precision scale

Top view

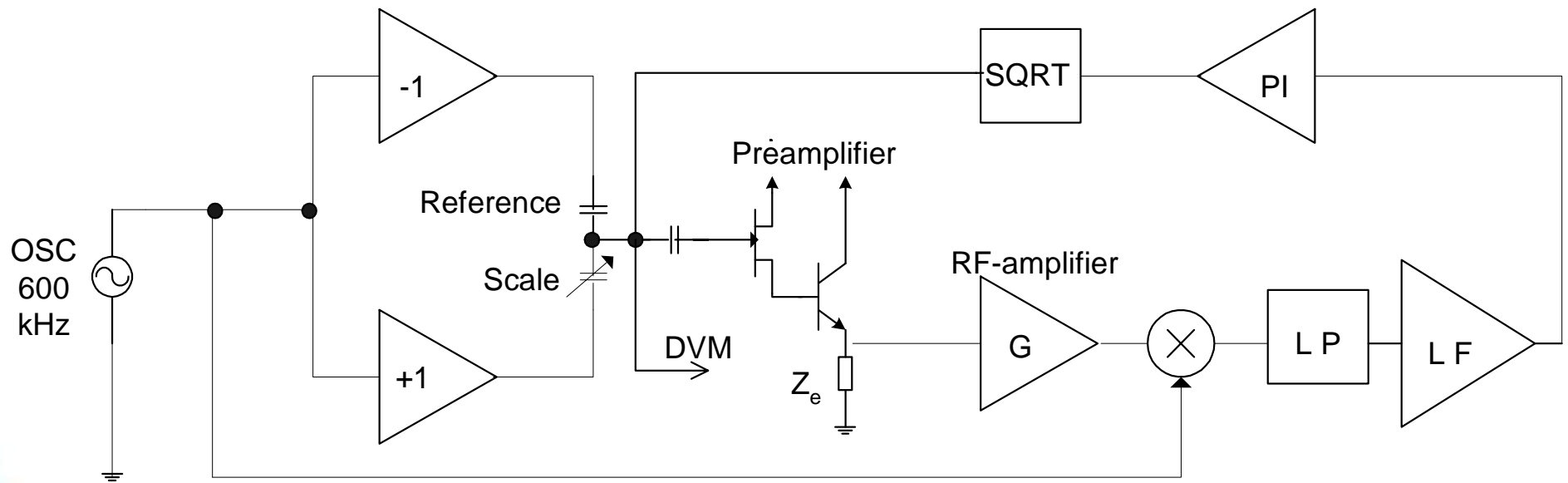


Exploded view



*VTT Automation, VTT Electronics, MIKES*

## (First) prototype electronics for the precision scale



## Brownian Noise of Capacitive Sensors

### DYNAMICS OF MEMS CAPACITOR

$$m \frac{d^2 x}{dt^2} + \eta \frac{dx}{dt} + kx = \frac{\epsilon A}{2(d-x)^2} (V + V_n)^2 + F_{mech} + F_n$$

$F_{mech}$  is a mechanical force (f.ex., gravity)

$V_n$  is the voltage noise  $\langle V_n(t)V_n(t+\tau) \rangle = 2k_B T R \delta(\tau)$

$F_n$  is the force noise  $\langle F_n(t)F_n(t+\tau) \rangle = 2k_B T \eta \delta(\tau)$

- Nonlinear dynamics ( $\Rightarrow$  mixing effects)
- Coupling between electrical and mechanical noise



## From friction to noise

Linearized system:  $x_\omega = G(\omega) f_\omega$

$$\text{Transfer function } G(\omega) = \frac{\omega_0^2 / k}{\omega_0^2 - \omega^2 + i\omega_0\omega / Q},$$

$$\omega_0 = \sqrt{\frac{k}{m}}$$

Thermal noise

$$\frac{1}{2}k_B T = \frac{1}{2}k \overline{x_n^2} \quad \text{Brownin liike}$$

$$\overline{x_n^2} = \frac{\overline{f_n^2}}{k^2} \int_0^\infty \frac{\omega_0^4}{(\omega_0^2 - \omega^2)^2 + (\omega_0\omega / Q)^2} \frac{d\omega}{2\pi} = \frac{\overline{f_n^2}}{f_n^2} \frac{\omega_0^4 Q}{4k^2} = \frac{k_B T}{k}$$

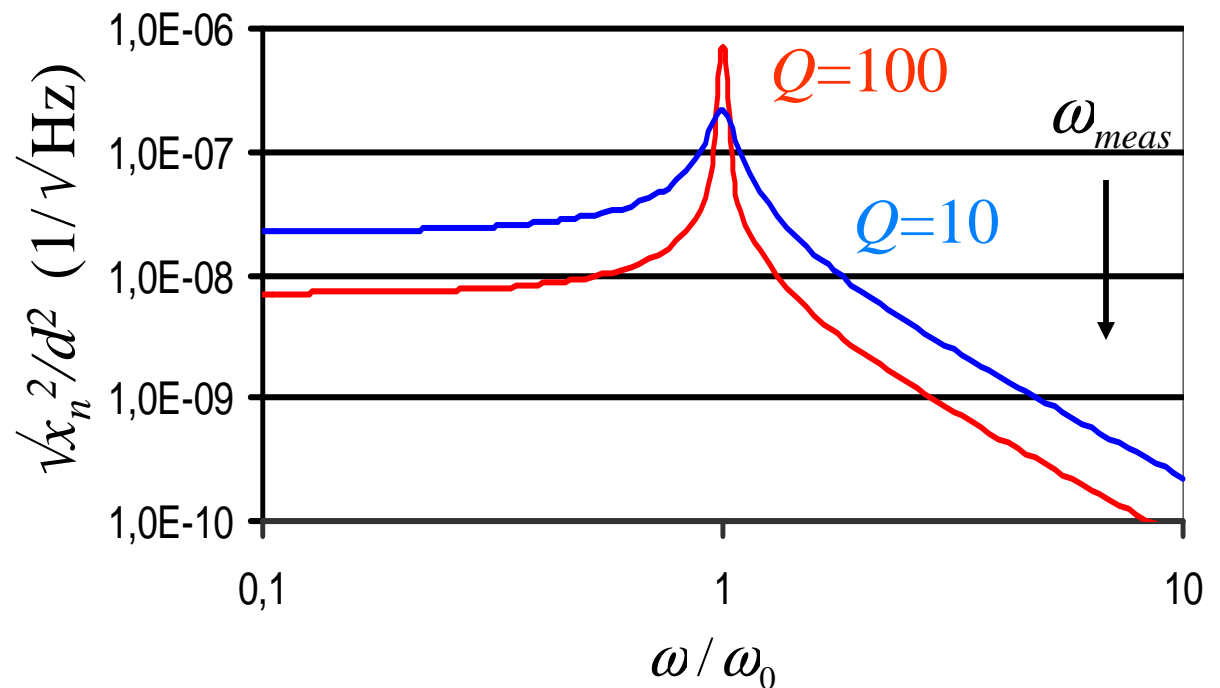
$$\overline{f_n^2} = \sqrt{4k_B T \eta} \quad (\text{White force noise assumed})$$

$\eta$  on kitkakerroin,  $\eta = \frac{k}{Q\omega_0}$ ,  $Q$  on mekaaninen hyvyysluku

## Mechanical noise

$$\frac{x_n^2 / d^2}{\Delta f} = \frac{4Qk_B T}{\omega_0 k d^2} \text{ at } \omega = \omega_m$$
$$= \frac{4k_B T}{Q\omega_0 k d^2} \text{ at } \omega = 0$$

### Displacement noise



**Low-freq noise decreases by increasing  $Q$  (= decreasing friction)  
(vacuum encapsulation)**

## Signal-to-noise

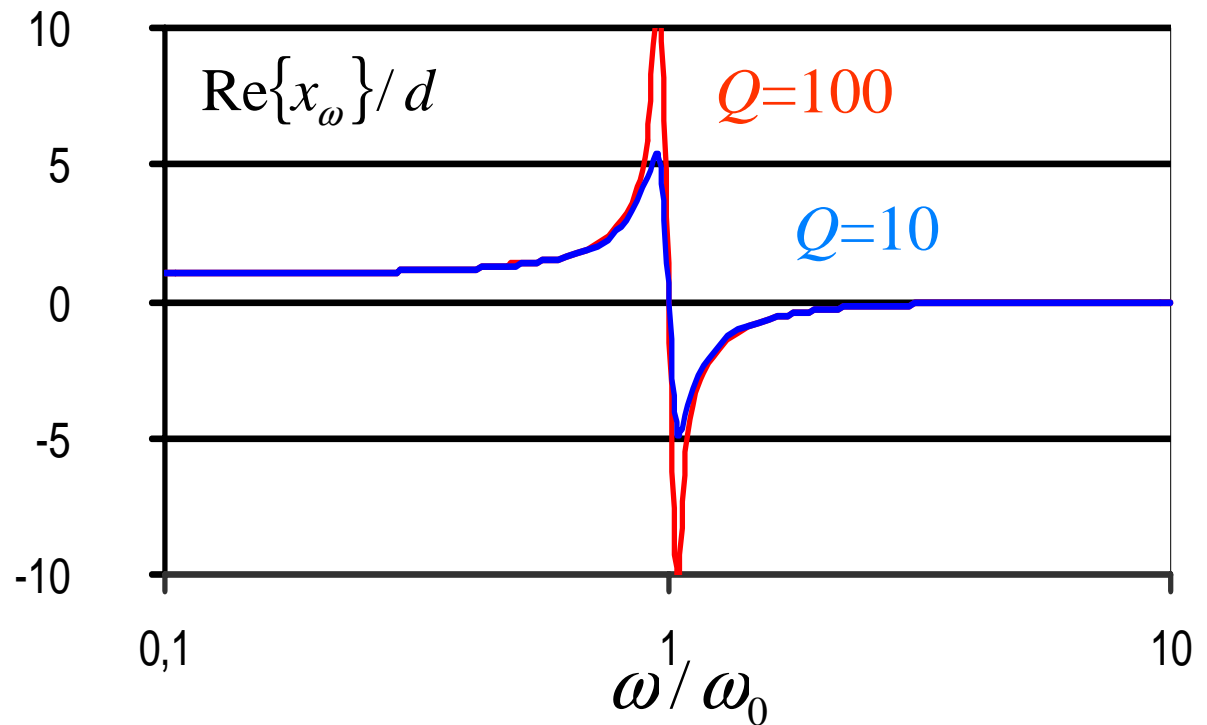
*Intrinsic only!*

$$\frac{\text{Re}\{x_\omega\}}{d} = \frac{1 - \omega^2 / \omega_0^2}{(1 - \omega^2 / \omega_0^2)^2 + (\omega / \omega_0 Q)^2} \frac{\text{Re}\{f_\omega\}}{kd}$$

$$\begin{aligned} \frac{S}{N} &= \frac{x/d}{\sqrt{x_n^2/d^2}} \\ &= \frac{\sqrt{\frac{Q\omega_0}{k}} F}{\sqrt{4k_B T \Delta f}} \end{aligned}$$

at low frequencies

*Other noise sources!*



# Signal-to-noise is the important quantity Not signal itself (i.e. sensitivity)

*Capacitive sensor has an internal noise mechanism which arises from internal energy dissipation.*

*It is temperature dependent.*

*It can be quantitatively predicted !*

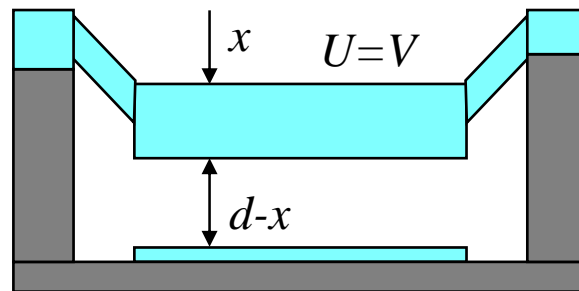
*Magnitude of the noise can be calculated from the equipartition theorem  $\frac{1}{2} kx^2 = \frac{1}{2} k_B T$  and the equation of motion for the released membrane of the capacitive sensor.*

*The latter determines how noise is shaped with frequency.*

## Electrostatic actuation (the concept of transducer)

## Actuation (i.e. movement) of the released electrode by using electrostatic force

$$F_{el} = F_{spring} \quad \Leftrightarrow \quad \frac{\epsilon_0 AV^2}{2(d-x)^2} = kx$$

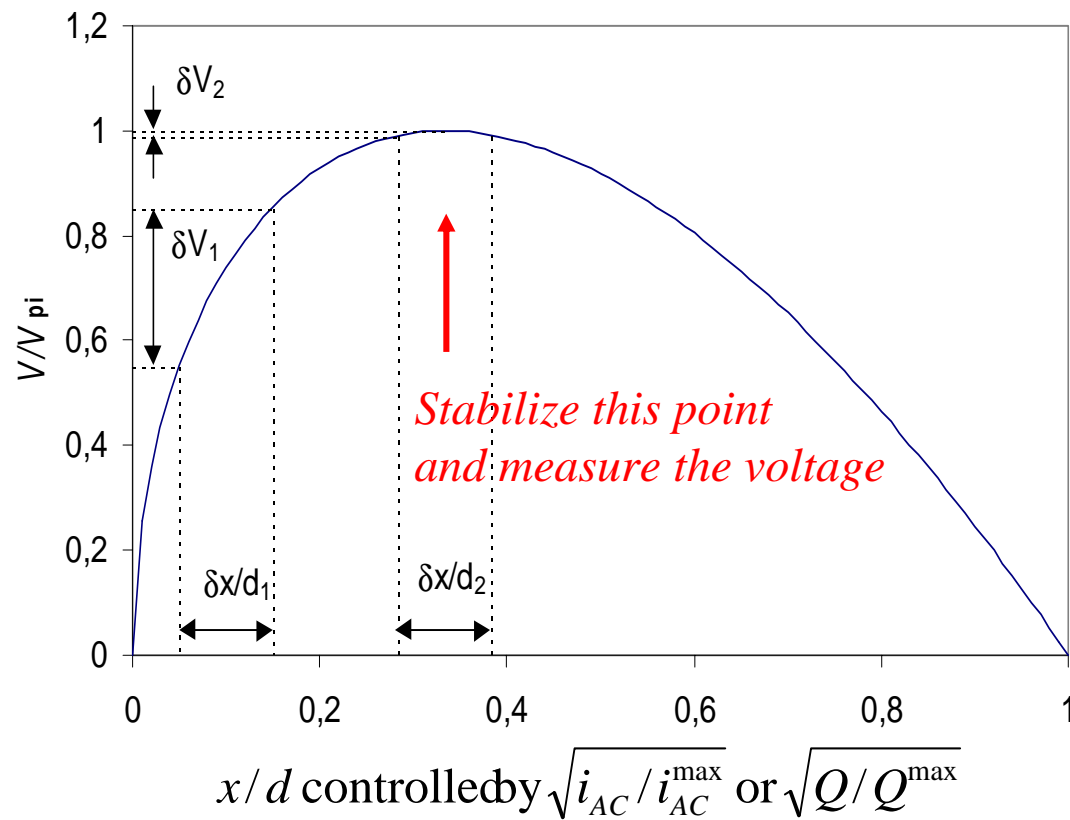


$$U=0$$

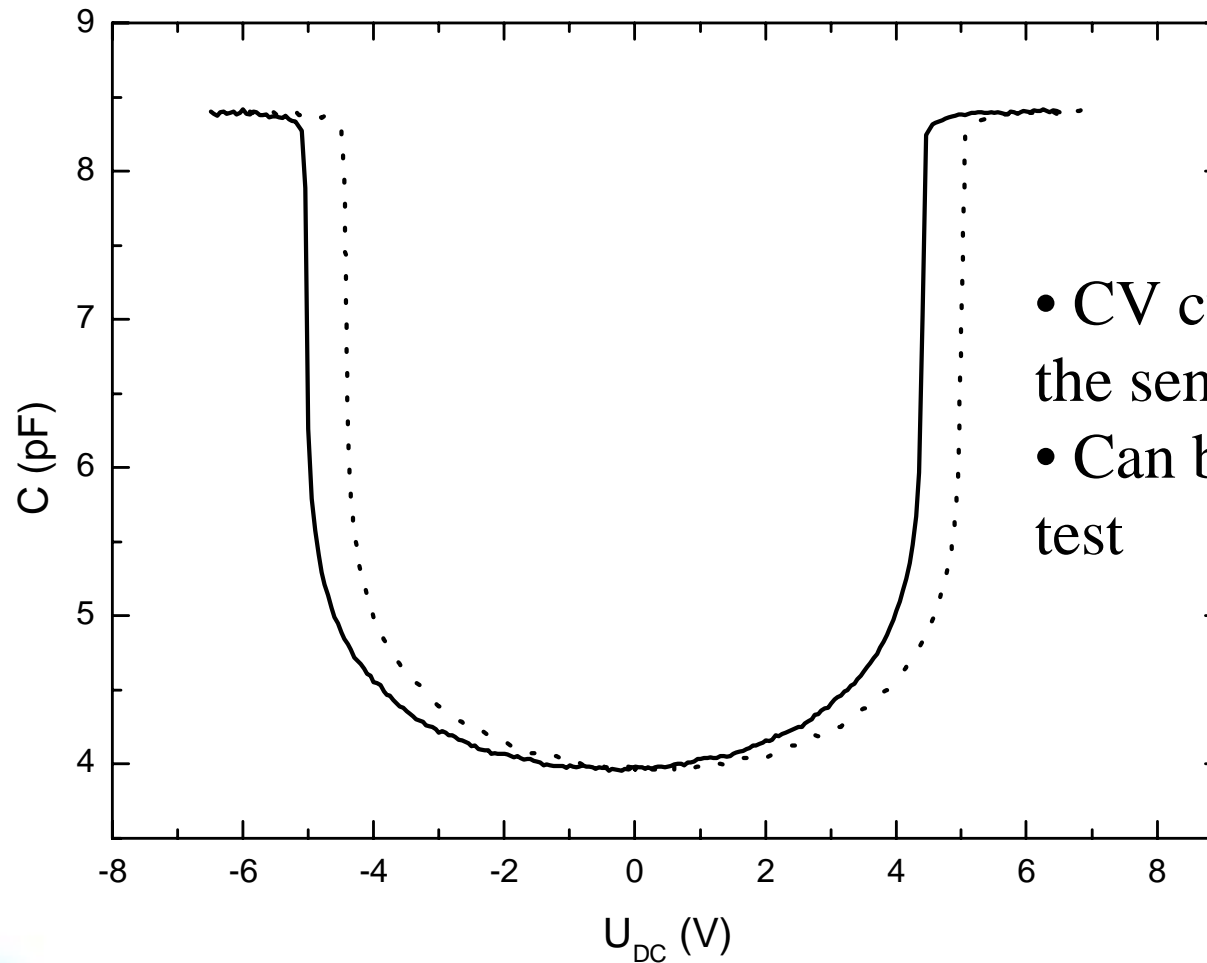
$$\text{Pull in at } V_{pi} = \sqrt{\frac{8kd^2}{27C_0}}$$

The electrodes are snapped together due to the nonlinearity of the electrostatic force

## “Eigencurve” of a moving parallel plate capacitor



## CV curve of a moving plate capacitor



- CV curve shows that the sensor is working
- Can be used for self test



## Miscellaneous

### Literature

1. **Stanfordin** tänään kevään “Introduction to Sensors” kurssi  
<http://design.stanford.edu/Courses/me220/me220.html>
2. **M. Elwenspoek, R. Wiegerink: “Mechanical Microsensors”**, Springer 2001 (*contains no S/N analysis!!!*)
3. **Universal capacitive readout (= general purpose ultra-low noise CMOS ASIC, contact [info@microsensors.com](mailto:info@microsensors.com))**
4. **Y. Netzer, “The Design of Low-Noise Amplifiers”, Proc. IEEE Vol. 69, No. 6, p. 728 – 741 (1981).**

<http://design.stanford.edu/Courses/me220/list.html#notes>

- Lecture 1: Human/Animal Sensors
- Lecture 2: Sensor Performance Characteristics
- Lecture 3: Strain Gauges
- Lecture 4: Capacitive Sensors and Accelerometer Fundamentals
- Lecture 5: ADXL50 Micromachine Accelerometer Demonstration
- Lecture 6: Piezoelectric Sensors
- Lecture 7: Pressure Sensors
- Lecture 8: Thermometers
- Lecture 9: Flow Sensors
- Lecture 10: Radiation Sensors
- Lecture 11: IR Sensors Demo: IR Motion
- Lecture 12: Inductive and Magnetic Sensors
- Lecture 13: Active Sounding Measurement Techniques Examples
- Lecture 14: DC Motor Demonstration
- Lecture 15: Micromachine Sensor Design and Fabrication
- Lecture 16: Chemical Sensors
- Lecture 17: Gyroscopes

## Other (RF) MEMS courses

- Prof. Antti Räisänen RF-MEMS kurssi
- International master's program on RFMEMS through the AMICOM Network of Excellence (Advanced MEMS for communications)
- VTT is a partner in this network
- Contact persons: [jussi.tuovinen@vtt.fi](mailto:jussi.tuovinen@vtt.fi), [aarne.oja@vtt.fi](mailto:aarne.oja@vtt.fi)